

CAE package for electromagnetic and thermal analysis using finite elements

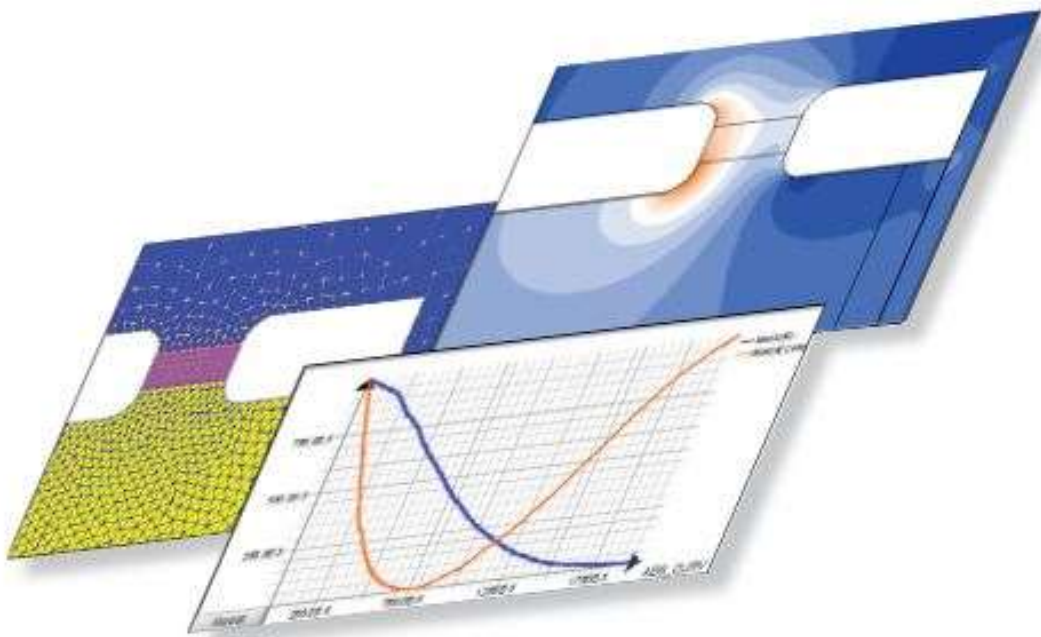
# Altair® Flux®

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## Electrostatic application tutorial

### 2D technical example



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## Foreword

\*(Please read before starting this document)

**Description of the example** The goal of this technical example is to demonstrate the ability and advantage of Flux for the simulation of cylindrical cell computation problems. This example contains the general steps and all the data needed to describe the different simulations.

**To begin** This example is designed for the user who is already familiar with the basic functions of Flux software.  
For beginner users, please report to the “Flux Starting Guide” opened automatically by the supervisor. (If not opened, please open it by clicking on the button “?” on the top right of the supervisor). The interface contains videos, which helps the beginners while using Flux for the first time.

**Support files included...** To view the completed stages of the example project, the user will find the .py files, including the geometry, mesh, physics and post-processing descriptions. The .py files corresponding to the different study cases in this example are available in the folder:  
.\DocExamples\Examples2D\Tutorial\_Technical\ElectrostaticApplication\  
Supplied files are command files written in Pyflux language. The user can launch them in order to automatically produce the Flux projects for each case.

*\*\*(py files are launched by accessing **Project/Command file** from the Flux drop down menu.)*

Supplied files		Contents	Flux file obtained after launching the .py file
CASE1	buildGeomesh.py	Geometry and mesh	...\geomeshbuilt
	buildphys.py	physics	...\physbuilt
	solving.py	Solving process	...\solved
	postprocessing.py	Post processing	...\postprocessed
CASE2	TESTCASE_INI.FLU	Initial Flux project	
	buildphys.py	Physics	...\physbuilt
	solving.py	Solving process	...\solved
	postprocessing.py	Post processing	...\postprocessed
CASE3	TESTCASE_INI.FLU	Initial Flux project	
	buildPhys.py	physics	...\physbuilt
	solving.py	Solving process	...\solved
	postprocessing.py	Post processing	...\postprocessed

Note : some directories may contain a main.py enabling the launch of the other command files



# Table of Contents

1. General information .....	1
1.1. Overview .....	3
1.1.1. Description of the studied device.....	4
1.1.2. Studied cases .....	6
1.2. Strategy to build the Flux project .....	7
1.2.1. Main stages for geometry description.....	8
1.2.2. Main stages for mesh generation .....	10
1.2.3. Main stages for physical description.....	11
2. Construction of the Flux project.....	13
2.1. Geometry description process .....	15
2.2. Mesh generation process.....	21
2.2.1. Mesh the device.....	22
2.2.2. Modify the aided deviation .....	23
2.2.3. Modify the mesh point and assign it to points .....	24
2.2.4. Create and assign relaxation on faces and lines.....	25
2.2.5. Mesh lines and faces .....	27
2.3. Physical description process.....	29
2.3.1. Create materials .....	30
2.3.2. Create face regions .....	31
2.3.3. Assign face regions to faces.....	32
2.3.4. Create line regions.....	33
2.3.5. Assign line regions to lines .....	34
3. Case 1: static study.....	35
3.1. Case 1: solving process .....	37
3.2. Case 1: results post-processing.....	39
3.2.1. Display default graphic post processing .....	40
3.2.2. Display arrows of the electric field on a region boundaries .....	42
3.2.3. Compute the electric potential on a point .....	43
3.2.4. Compute the energy on LIQUID region .....	44
3.2.5. Plot a 2D curve of the electric field variation along a path .....	45
3.2.6. Plot a 2D curve of normal and tangential components of the electric field along a path.....	47
3.2.7. Plot a 2D curve of the electric field along a path .....	48
4. Case 2: multi-parametric computation.....	51
4.1. Case 2: physical description .....	53
4.1.1. Create an I/O parameter.....	54
4.1.2. Modify a material .....	55
4.1.3. Create sensors .....	56
4.2. Case 2: solving process .....	57
4.3. Case 2: results post-processing.....	59
4.3.1. Display default graphic post processing at a selected parametric step .....	60
4.3.2. Create animation of isovalues of the electric field on face regions versus I/O parameter .....	61
4.3.3. Plot a 3D curve of the electric field at a point versus I/O parameters .....	62
4.3.4. Plot a 3D curve of the potential at a point versus I/O parameters.....	63
4.3.5. Plot a 3D curve of electric field along a path versus I/O parameter .....	64
4.3.6. Plot a 2D curve of the energy versus I/O parameter .....	66
5. Case 3: static study, material with the low relative permittivity .....	67
5.1. Case 3: modifying physical properties .....	69
5.1.1. Create a material .....	70
5.1.2. Modify the LIQUID face region .....	71
5.2. Case 3: solving process .....	73
5.3. Case 3: results post-processing.....	75
5.3.1. Display isolines of the electric potential on face regions .....	76
5.3.2. Plot a 2D curve of the electric field along a path .....	77

5.3.3. Import and superimpose 2D curve..... 79

5.3.4. Compute the energy on LIQUID region ..... 81



# 1. General information

---

**Introduction** This chapter contains the presentation of the **studied device** and the **Flux software**.

---

**Contents** This chapter contains the following topics:

Topic	See Page
Overview	3
Strategy to build the Flux project	7

---



## 1.1. Overview

---

### Introduction

This section presents the studied device (a cylindrical cell for the measurement of resistivity and permittivity of liquids) and the strategy of the device description in Flux.

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### Contents

This section contains the following topics:

Topic	See Page
Description of the studied device	4
Studied cases	6

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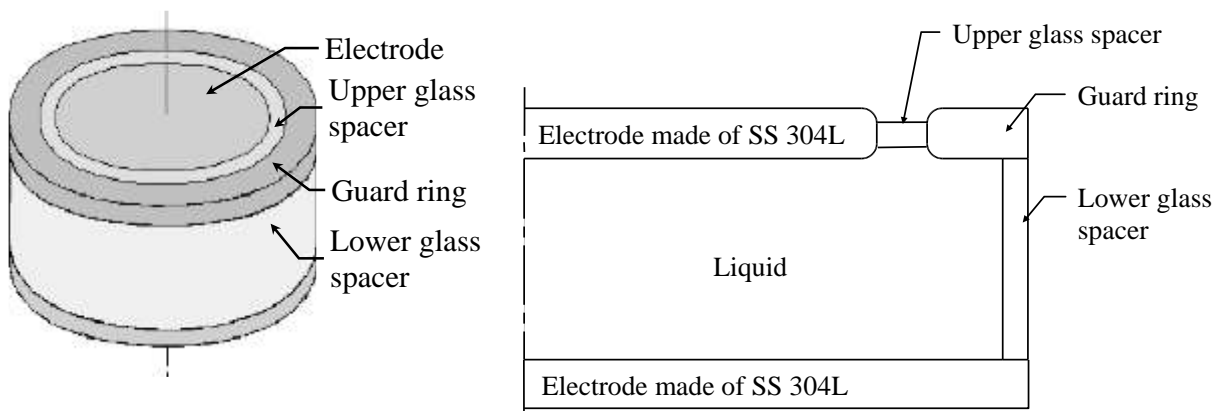
### 1.1.1. Description of the studied device

**Studied device** The device to be analyzed is a cylindrical cell for the measurement of resistivity and permittivity of liquids.

The studied device consists of:

- two circular upper and lower electrodes
- a guard ring
- two glass spacers
  - one is situated between the upper electrode and the guard ring
  - another is situated between the guard ring and the lower electrode

The physical model and the axial section of the studied device are presented in the figures below.



#### Operating principle

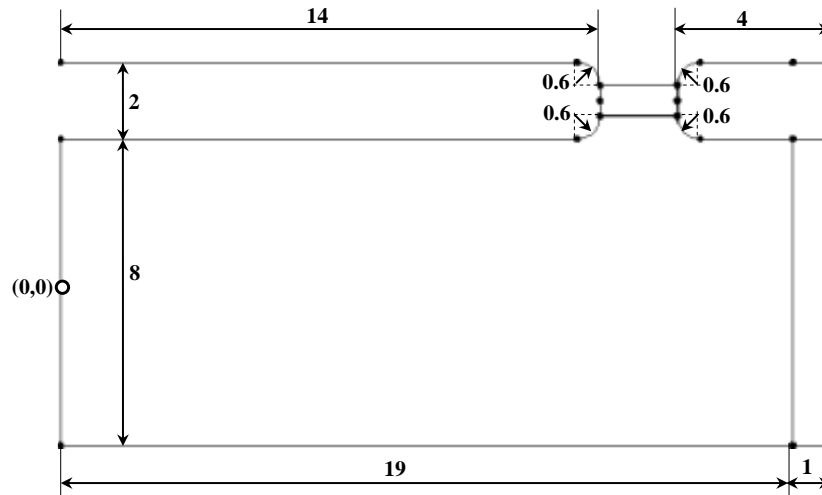
The analyzed cell is used to measure the resistivity and permittivity of liquids. The testing liquid is placed between two plate electrodes to form a capacitor. The measured capacitance is then used to calculate permittivity. When simply measuring the dielectric material between two electrodes, stray capacitance or edge capacitance is formed on the edges of the electrodes and consequently the measured capacitance is larger than the capacitance of the dielectric material. A solution to the measurement error caused by edge capacitance is to use the guard electrode. The guard electrode absorbs the electric field at the edge and the capacitance that is measured between the electrodes is only composed of the current that flows through the dielectric material.

*Continued on next page*

## Geometry

The device has an axial symmetry around its main axis.

The dimensions (in millimeters) of the device are presented in the figure below.



## Materials

The measurement cell is composed of the following materials:

- the upper and lower electrodes are made of SS 304L, an austenitic Chromium-Nickel stainless steel
- the upper and lower spacers are made of glass, an insulator characterized by the constant relative permittivity

The testing liquids are:

- pure water
- mineral oil, a material with a high dielectric constant

## Sources

The electric field is due to the dc voltage applied to electrodes as follows:

- $V = -250$  V on the lower electrode
- $V = 250$  V on the upper electrode

## 1.1.2. Studied cases

---

**Studied cases**

Three cases are carried out in a Electro Static application:

- case 1: static study, a testing liquid is pure water
  - case 2: multi-parametric computation
  - case 3: static study, a testing liquid is mineral oil
- 

**Case 1**

*The first case is a static study.*

This study is a very easy problem of electrostatics of axisymmetric type. The testing liquid is pure water.

---

**Case 2**

*The second case is a multi-parametric computation.*

In this study two parameters – physical and geometric – are used. The physical parameter is the relative permittivity of the testing liquid (pure water) varying between 10 and 120. The geometric parameter is the curvature radius of the rounded corners of the electrodes varying between 0.6 mm and 0.8 mm. The last parameter determines the height of the upper glass spacer. The height of the upper spacer decreases when the value of the curvature radius increases.

---

**Case 3**

*The third case is a static study.*

This study differs from case 1 only by the nature of the testing material. The testing liquid is mineral oil.

---

## 1.2. Strategy to build the Flux project

---

### Introduction

This section presents outlines of the geometry building process, mesh generating process and physical properties description process of the measurement cell.

---

### Contents

This section contains the following topics:

Topic	See Page
Main stages for geometry description	8
Main stages for mesh generation	10
Main stages for physical description	11

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### Preliminary

Before starting the project construction, we must define the application with which the calculation will be made: the **2D Electro Static application**.

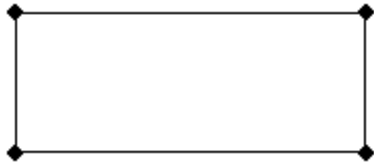
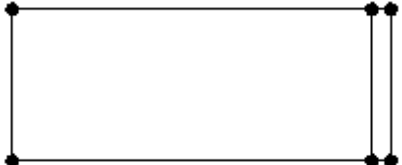
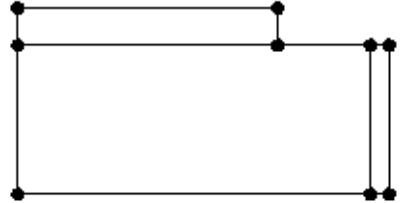

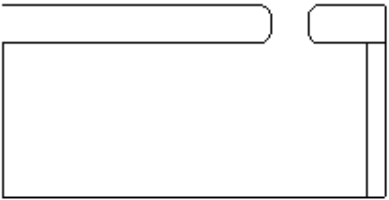
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## 1.2.1. Main stages for geometry description

### Outline

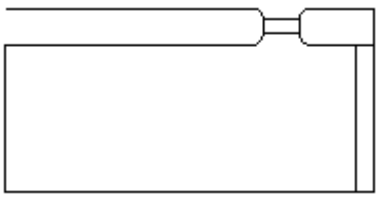
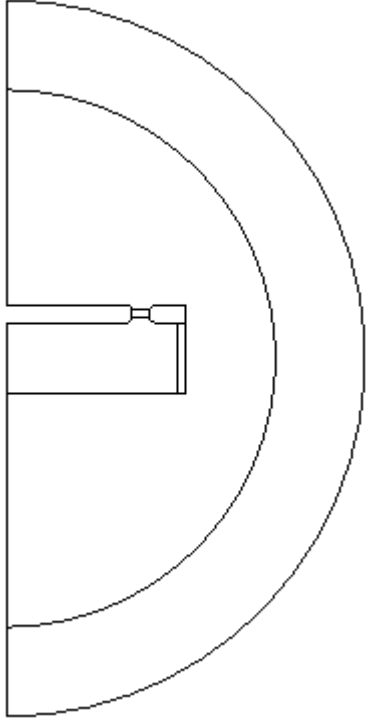
The device is modeled in the axisymmetric study domain, i.e. the device is described in a XY-plane cross-section and has symmetry with respect to the Y-axis. The lower electrode is modeled by physical line region, it is not necessary to build its geometry.

An outline of the **geometry building process** of the measurement cell is presented in the table below.

Stage	Description	
1	Creation of geometric parameters to simplify the geometry construction	<ul style="list-style-type: none"> <li>• RADIUS (curvature radius of the corners of the upper electrode and guard ring): 0.6 mm</li> <li>• RINF_EXT (outer radius of the infinite box): 40 mm</li> <li>• RINF_INT (inner radius of the infinite box): 30 mm</li> </ul>
2	Creation of the liquid part	
3	Creation of the lower glass spacer	
4	Creation of the electrode	
5	Creation of the guard ring	
6	Modification of the geometry of the electrode and guard ring, Creation of some fillets	

*Continued on next page*

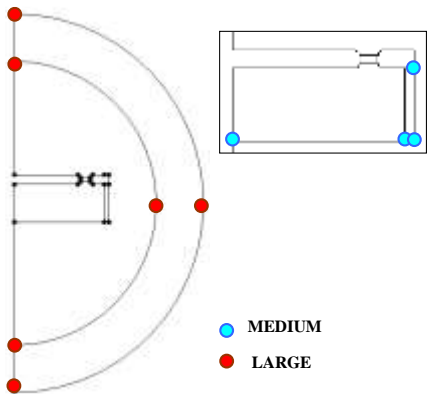
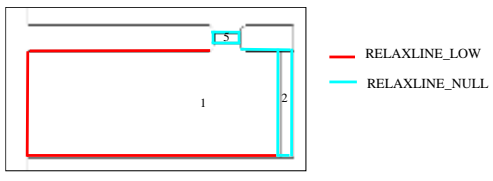
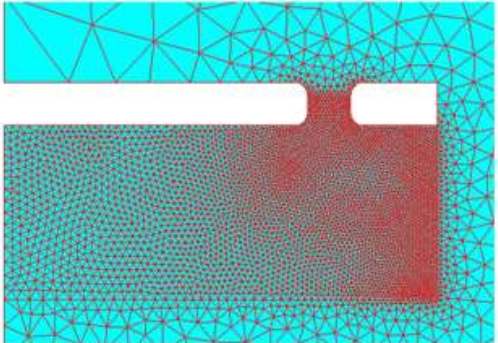


7	Creation of the upper glass spacer	
8	Creation of the infinite box and closing the domain.	

## 1.2.2. Main stages for mesh generation

### Outline

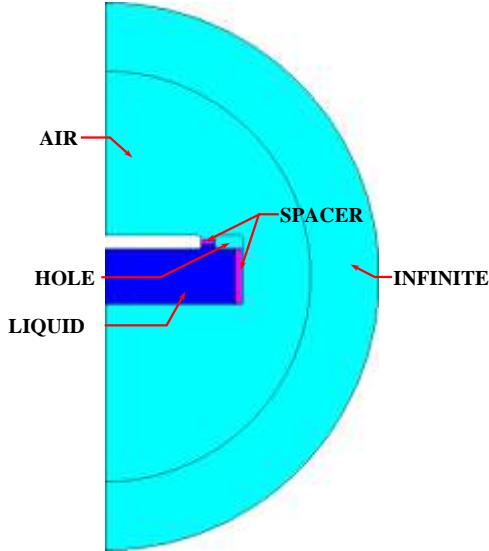
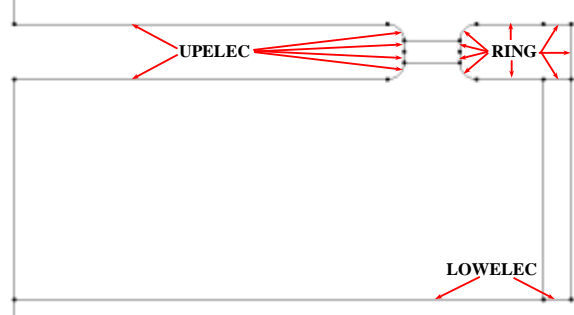
An outline of the **mesh generating process** of the measurement cell is presented in the table below.

Stage	Description	
1	Meshing the device and analyze of the mesh	Mesh with the default settings of AIDED MESH. It is possible to improve the mesh quality
2	Modify aided mesh information	Aided mesh information are modified to improve the global mesh
3	Assign local meshpoint	 <p>● MEDIUM ● LARGE</p>
4	Assign local relaxation on lines (see figure) and faces 1, 2 and 5	 <p>— RELAXLINE_LOW — RELAXLINE_NULL</p>
5	Meshing: • meshing lines • meshing faces	

### 1.2.3. Main stages for physical description

#### Outline

An outline of the **physical description process** of the measurement cell is presented in the table below.

Stage	Description	
1	Creation of 2 materials	<ul style="list-style-type: none"> <li>• WATER – isotropic material with a linear dielectric characteristic</li> <li>• GLASS – isotropic material with a linear dielectric characteristic</li> </ul>
2	Creation and assignment of face regions	
3	Creation and assignment of line regions	



## 2. Construction of the Flux project

---

**Introduction** This chapter contains the **geometry description**, **mesh generation** and **physical description** of the **measurement cell** presented in a manner less detailed than the chapters relating to the studied cases. The user must have good understanding of all functionalities of the Flux preprocessor.

---

**Project name** The Flux project is **GEO\_MESH\_PHYS.FLU**.

---

**Contents** This chapter contains the following topics:

Topic	See Page
Geometry description process	15
Mesh generation process	21
Physical description process	29

---

**Preliminary** First, the physical application is defined. The required physical application is the Electro Static 2D application.  
The characteristics of the application are presented in the table below.  
Remark: Before, close Sketcher context if it is automatically opened.



Project → CloseSketcher2DContext

Electro Static 2D application	
Definition	
2D domain type	Reference for potential (infinity, symmetry...)
Axisymmetric	Floating potential



Application → Define → Electric → Electro Static 2D

---



## 2.1. Geometry description process

Geometry  
description

Mesh  
generation

Physic  
description

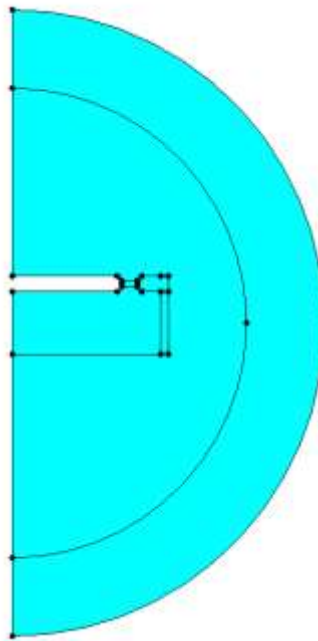
Solving  
process

Result  
post-processing

### Introduction

This section presents the general steps of the geometry construction and the data required to describe the measurement cell geometry.

The cell object is presented in the figure below.



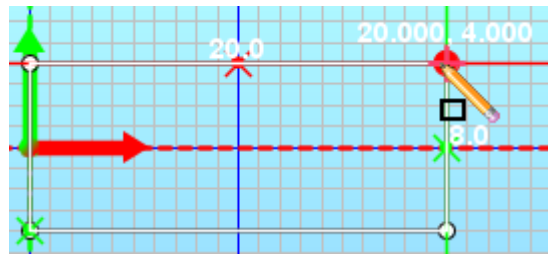

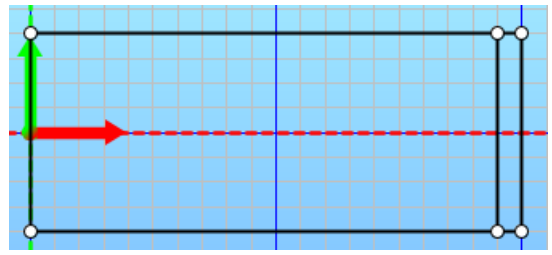

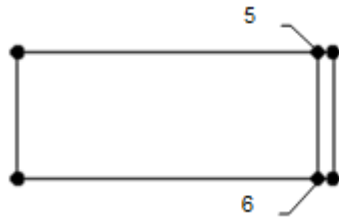



### Goal

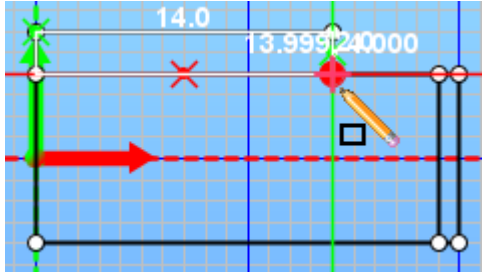


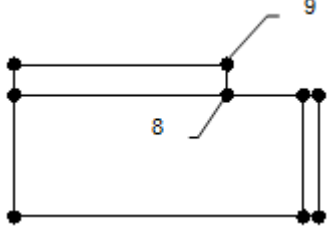





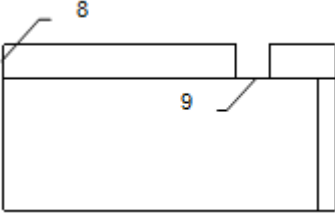


The geometry is created in the Sketcher using rectangle, line creation and geometric parameters.

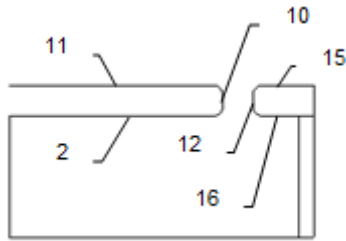


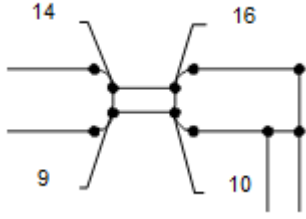


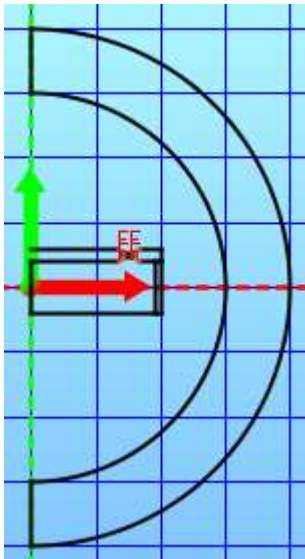


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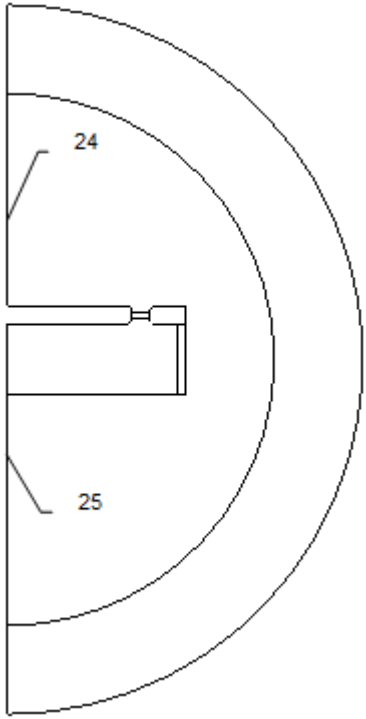


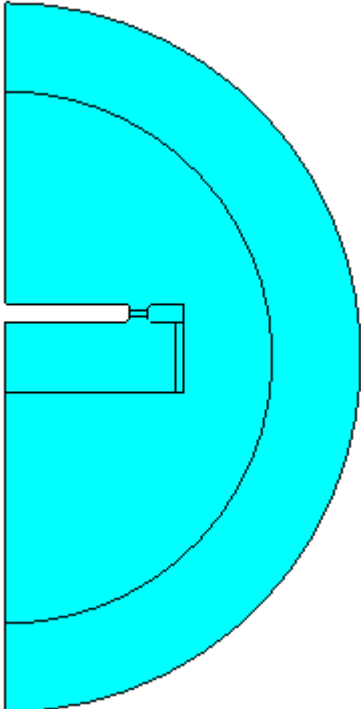


**Action** The steps of the construction of the cell are presented in the following table.

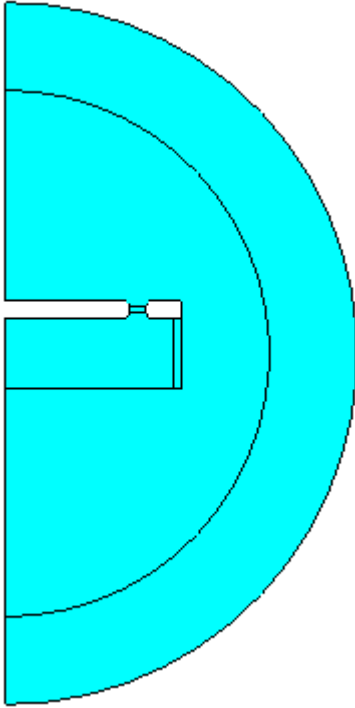


Step	Action		Illustration
0	Open sketcher context		
		Geometry → Sketcher 2D context	
1	Creation of geometric parameters		<ul style="list-style-type: none"> <li>• RADIUS (curvature radius of the corners of the upper electrode and guard ring): 0.6 mm</li> <li>• RINF_EXT (outer radius of the infinite box): 40 mm</li> <li>• RINF_INT (inner radius of the infinite box): 30 mm</li> </ul>
		Construction → Geometric parameter → New	
2	Creation of a rectangle by a diagonal between a first point (0 ; -4) and a second point (20 ; 4) dimensions of 20 x 8.		
		Construction → Rectangle → Rectangle diagonal	
3	Creation of a second rectangle inside the first one in order to create the lower glass spacer. (first point : 19 ; 4, second point : 20; -4)		
		Construction → Rectangle → Rectangle diagonal	
4	Verify the coordinates of the selected points		
		Select points, right click and choose Edit array	



5	<p>Creation of a rectangle in order to create the electrode (first point : 0 ; 6, second point : 14 ; 4)</p>										
	<p> <b>Construction → Rectangle → Rectangle diagonal</b></p>										
6	<p>Verify the coordinates of the selected points</p> <table border="1" data-bbox="319 730 852 842"> <thead> <tr> <th>Flux point</th><th>X</th><th>Y</th></tr> </thead> <tbody> <tr> <td>8</td><td>14</td><td>4</td></tr> <tr> <td>9</td><td>14</td><td>6</td></tr> </tbody> </table>	Flux point	X	Y	8	14	4	9	14	6	
Flux point	X	Y									
8	14	4									
9	14	6									
	<p> <b>Select points, right click and choose Edit array</b></p>										
7	<p>Creation of a rectangle in order to model the guard ring (first point : 16 ; 6 and second point : 20 ; 4)</p>										
	<p> <b>Construction → Rectangle → Rectangle diagonal</b></p>										
8	<p>Deletion of lines 8 and 9</p>										
	<p> <b>Select lines, right click and choose Delete</b></p>										

9	Creation of four fillets in order to model four curved lines for the electrode and the guard line				
	Curved line	line	line		radius
	13	11	10		radius
	17	10	2		radius
	18	15	12		radius
	19	12	16		radius
		Tools → Fillet			
10	Creation of two lines to model the upper glass spacer.				
			Construction → Line → Polyline		
11	Creation of the infinite box of the disc type				
	Name	Internal radius	External radius		
	InfiniBox	RINF_INT	RINF_EXT		
		Select Domain → Infinite box → New			

12	<p>Creation of two lines in order to close the domain</p>	 <p>The diagram shows a cross-section of a semi-circular domain. A central rectangular structure is present. Two lines, labeled 24 and 25, are shown extending from the central structure towards the outer boundary, intended to close the domain.</p>
	 <b>Construction → Line → Polyline</b>	
13	<p>Closing of the sketcher context. The project opens in the geometry context of Flux and faces are automatically created.</p>	 <p>The diagram shows the same cross-section as in step 12, but now the entire area is filled with a solid cyan color, indicating that the sketcher context has been closed and the faces have been automatically created.</p>
	 <b>Select Project → CloseSketcher2DContext</b>	

14	Deletion of face 4.	
	Select the face, right click and choose Delete	

## 2.2. Mesh generation process

Geometry  
description

Mesh  
generation

Physic  
description

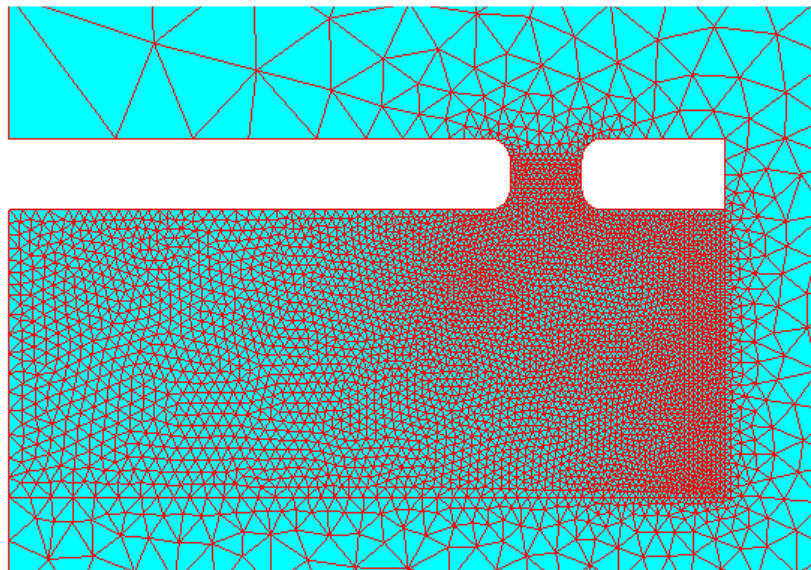
Solving  
process

Result  
post-processing

### Introduction

This section presents the general steps of mesh generation for the computation domain and the data required to describe the measurement cell mesh.

The meshed measurement cell is presented in the figure below.



### Contents

This section contains the following topics:

Topic	See Page
Mesh the device	22
Modify the aided deviation	23
Create and assign relaxation on faces and lines	25
Mesh lines and faces	27

## 2.2.1. Mesh the device

**Goal** Mesh generation process is an essential step of the Finite Element method. At this stage, the computation domain is divided in small elements. Each node of the mesh constitute a support where the **state variable** approximation (such as scalar or vector potentials, temperature, etc.) and the **derived fields** (such as magnetic field and induction, magnetic flux density, electric field, thermal flux density, etc.) are computed. Aided mesh is activated by default in Flux. Such tool permits to obtain a first basic mesh with global settings.

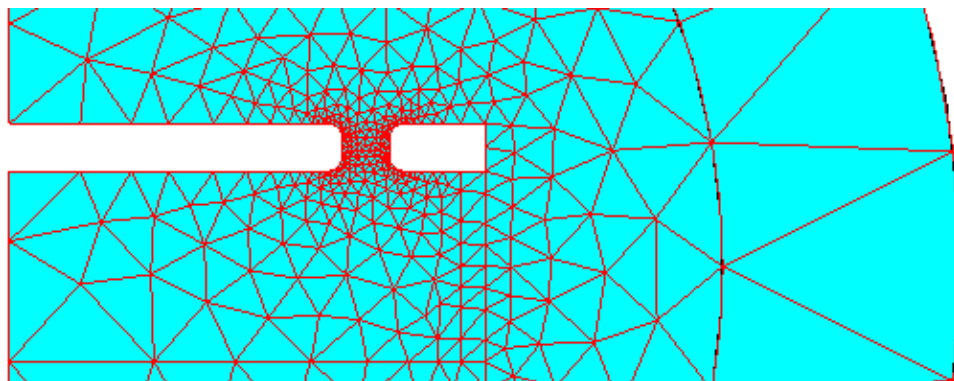
**Action** Mesh the device.



Mesh → Mesh domain



**Result** The result appears as below.



**Comments** To optimize the accuracy of the results, it is advised to have a mesh:

- with well proportioned mesh elements (close to equilateral triangle)
- with an Infinite box of at least 2 elements large
- taking into account the physics (the mesh must be denser in the areas with important field variation)

For instance, the solution to improve the mesh here is:

- to assign local mesh point
- to create and assign local relaxations on lines and faces
- to modify the aided deviation

## 2.2.2. Modify the aided deviation

**Goal** The aided deviation is modified in order to refine the mesh closed by the curved lines of the upper electrode and the guard ring.

**Data** The modified characteristic of the aided mesh is presented in the table below.

Deviation		
Assign	Type	Value
Assign – <b>Included</b> Infinite Box	Relative	<b>0.75</b>



Mesh → Aided Mesh → Edit



**Action** Mesh domain.



Mesh → Mesh domain



### 2.2.3. Modify the mesh point and assign it to points

#### Goal

Mesh points enable the user to add some local mesh information in order to control the mesh in specific areas. In this case:

- LARGE meshpoint permits to have an Infinite box with 3 elements large
- MEDIUM meshpoint permits to obtain a denser mesh in the device part

#### Data

The modified characteristics of the mesh points are presented in the table below.

Mesh point				
Name	Comment	Unit	Value	Color
LARGE	Large mesh size	mm	$(RINF\_EXT - RINF\_INT)/2.5$	Red
MEDIUM	Medium mesh size	mm	1.2	Turquoise



Mesh → Mesh point → Edit array

#### Action

Assign mesh point to points.

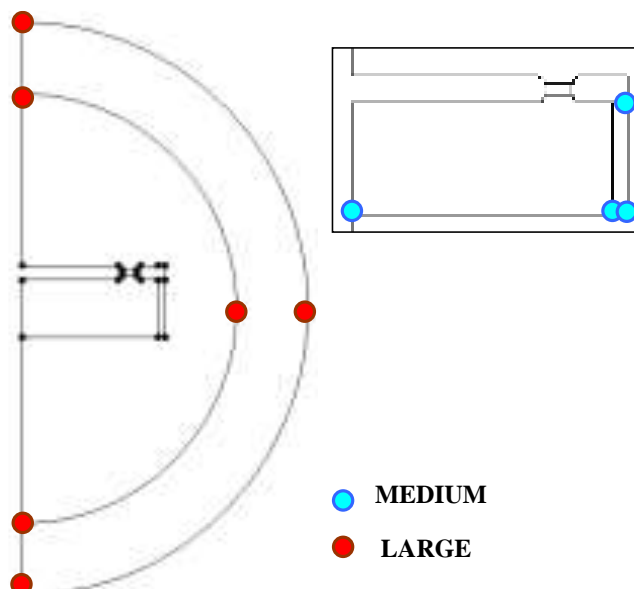


Mesh → Assign mesh information → Assign mesh point / line / generator → Assign mesh point to points



#### Outline

The assignment of the mesh points to points is presented in the figure below.





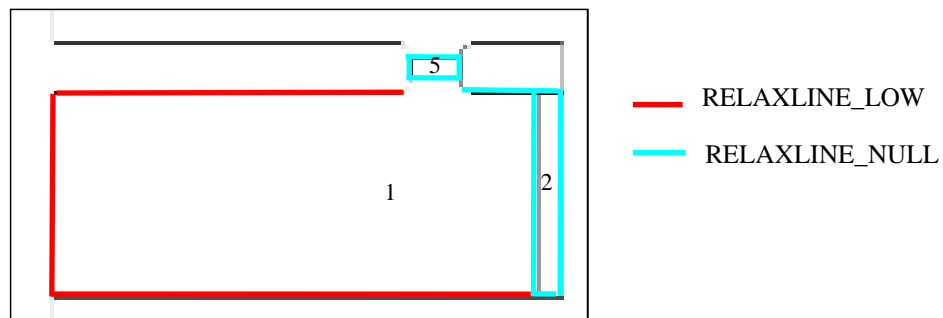
## 2.2.4. Create and assign relaxation on faces and lines

### Goal

Relaxation on faces and lines can be useful to control the harmonious progression of the mesh density from the smallest to the biggest mesh size element.

In our case, it is interesting to limit the relaxation effect on the device by imposing:

- a null relaxation on the lines surrounding the spacers
- a low relaxation on some lines surrounding face 1
- a null relaxation on faces 1, 2, 5. Elements located in the center of the liquid region (close to symmetry line) will be a little bigger.



### Data (1)

The characteristics of the relaxation on lines are presented in the table below.

Relaxation on lines			
Name	Comment	Value	Color
RELAXLINE_LOW	Low relaxation on lines	$r = 0.25$	Red
RELAXLINE_NULL	Null relaxation on lines	$r = 0.00$	Turquoise



Mesh → Relaxation → Relaxation line → New



### Action (1)

Assign relaxation to lines.



Mesh → Assign mesh information → Assign relaxation / shadow → Assign relaxation to lines



*Continued on next page*

**Data (2)**

The characteristics of the relaxation on face are presented in the table below.

Relaxation on faces			
Name	Comment	Value	Color
RELAXFACE_NULL	Null relaxation on faces	$r = 0.00$	Turquoise



Mesh → Relaxation → Relaxation face → New

**Action (2)**

Assign relaxation to face.



Mesh → Assign mesh information → Assign relaxation / shadow → Assign relaxation to faces



## 2.2.5. Mesh lines and faces

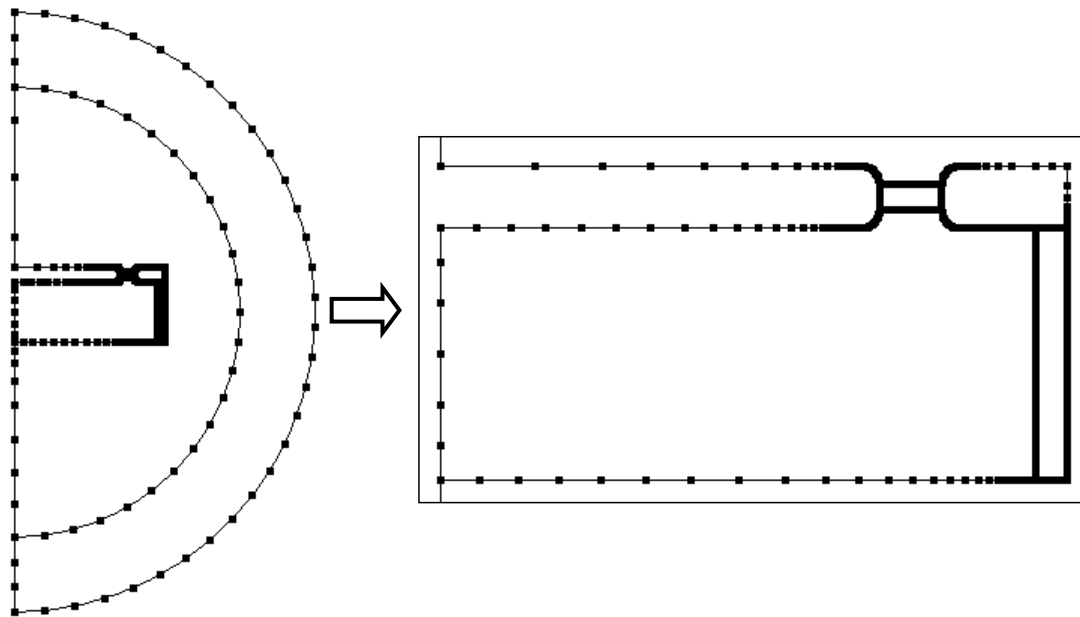
**Action (1)** Mesh lines.



Mesh → Mesh → Mesh lines



**Result (1)** After the lines have been meshed the next figure is displayed in the graphic zone.



**Action (2)** Mesh faces.



Mesh → Mesh → Mesh faces

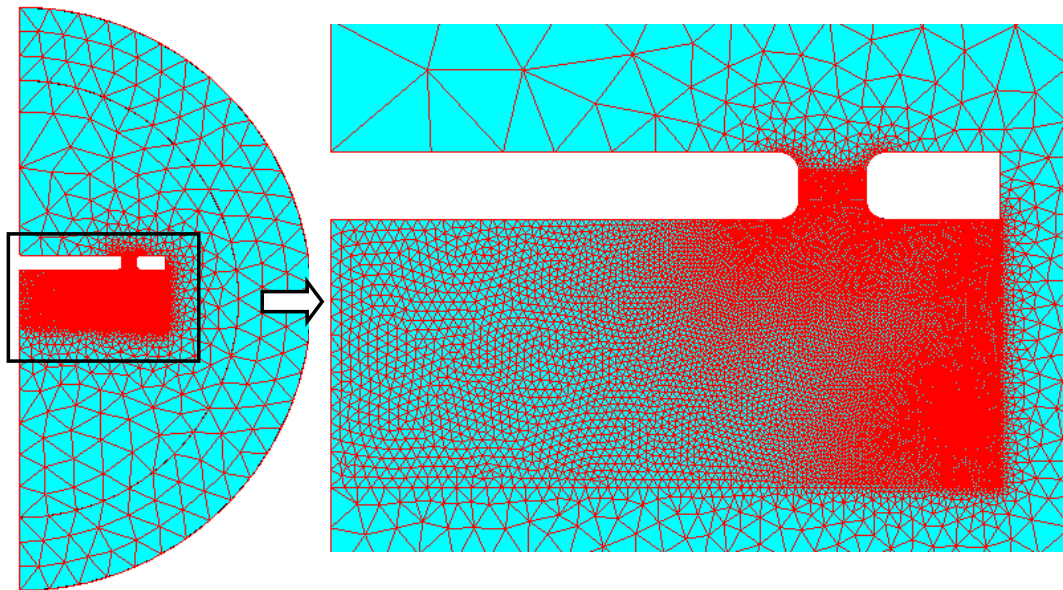


Note: another solution is to select the command Mesh domain.

*Continued on next page*

**Result (2)**

The mesh of the study domain and the detail of the mesh in the device zone are presented in the figure below.



The following comments will be displayed in the History zone.

Meshing of 5 faces

Automatic mesh of 25 lines

18:22:35 207 sec. Internal meshing of the lines

Automatic meshing of 5 faces

Boundary meshing of the faces achieved in 1 iteration(s)

Internal meshing of the 5 faces

Faces internal meshing achieved

Boundary meshing of the faces achieved in 1 iteration(s)

Internal meshing of the 5 faces

Faces internal meshing achieved

Boundary meshing of the faces achieved in 1 iteration(s)

Internal meshing of the 5 faces

Faces internal meshing achieved

End of topological mesh regularization

18:22:44 215 sec. 21340 1st order surfacic elements created

18:22:44 215 sec. Generating 2nd order elements is running

Total number of nodes --> 42934

18:22:44 216 sec. End generating 2nd order elements

Surface elements :

Number of elements not evaluated	: 0 %
Number of excellent quality elements	: 99.93 %
Number of good quality elements	: 0.06 %
Number of average quality elements	: 0 %
Number of poor quality elements	: 0 %
meshFaces executed	

**Comments**

The mesh takes into account geometry constraints. We also assume that the electric field with highest intensity and strongest variation will be located in the area between the two electrodes. The mesh must be denser in this area.

## 2.3. Physical description process

Geometry  
description

Mesh  
generation

Physic  
description

Solving  
process

Result  
post-processing

---

### Introduction

This section presents the definition of the physical properties – materials and regions of the model.

---

### Contents

This section contains the following topics:

Topic	See Page
Create materials	30
Create face regions	31
Assign face regions to faces	32
Create line regions	33
Assign line regions to lines	34

---

## 2.3.1. Create materials

### Goal

The creation of “material” entities enables the user to assign physical material properties to face regions. The two materials are linear isotropic characterized by the relative permittivity:

- the first material is water defined for the cell contents
- the second material is glass defined for the spacer

### Data

The characteristics of the materials are presented in the table below.

D(E) dielectric property: linear isotropic		
Name	Comment	Relative permittivity
WATER	Pure water at 20 degrees	80
GLASS	Classical glass	7

### Action

Create materials.



Physics → Material → New



## 2.3.2. Create face regions

### Introduction

Four face regions are necessary for the physical description of the measurement cell.

Four following face regions will be created:

- the LIQUID region corresponding with the contents of the cell
- the SPACER region for the upper and lower glass spacer
- the AIR region corresponding with the air surrounding the device
- The INFINITE region, already created during the infinite box creation, will be edited to activate its physical properties.

### Goal

Physical region are necessary to carry out the physical description of the model. They enable the user to group some entities (here faces grouped in face regions) that have the same physical properties. It is also possible to assign material and or conducting properties for instance.

### Data

The characteristics of the face regions are presented in the table below.

Face region				
Name	Comment	Type	Material/ conductor	Color
LIQUID	Contents of the cell	Dielectric region with charge source	WATER	Yellow
SPACER	Upper and lower glass spacer	Dielectric region with charge source	GLASS	Magenta
AIR	Air surrounding the device	Air or vacuum region	-	Cyan
INFINITE*	Infinite region	Air or vacuum region	-	Green

### Action

Create face regions.



Physics → Face region → New



\*The region already created and assigned during the creation of the infinite box.

### 2.3.3. Assign face regions to faces

**Introduction** The INFINITE region has been already assigned during the creation of the infinite box. The three face regions (LIQUID, SPACER, and AIR) are assigned to faces.

**Goal** The assignment operation enables the user to “link” the physical properties he has just created with the geometrics entities.

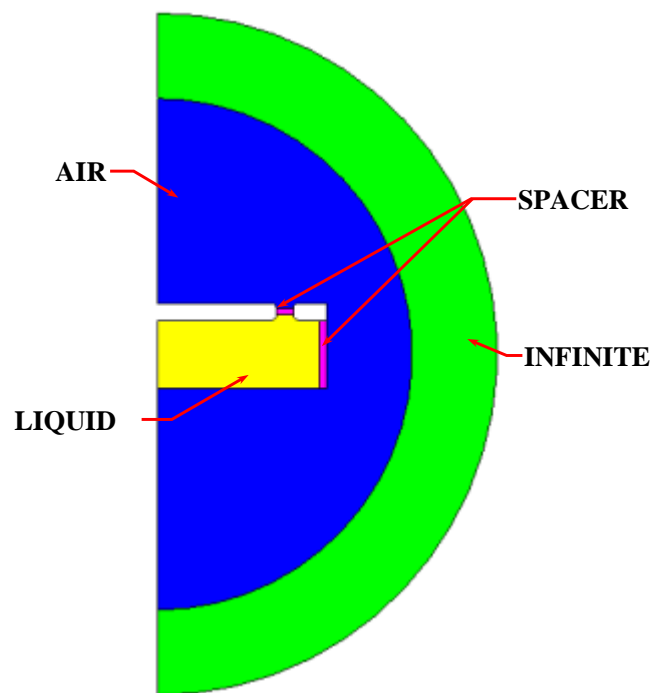
**Action** Assign face regions to faces.



Physics → Face region → Assign regions to faces  
(completion mode)



**Outline** The region assignment is presented in the figure below.





## 2.3.4. Create line regions

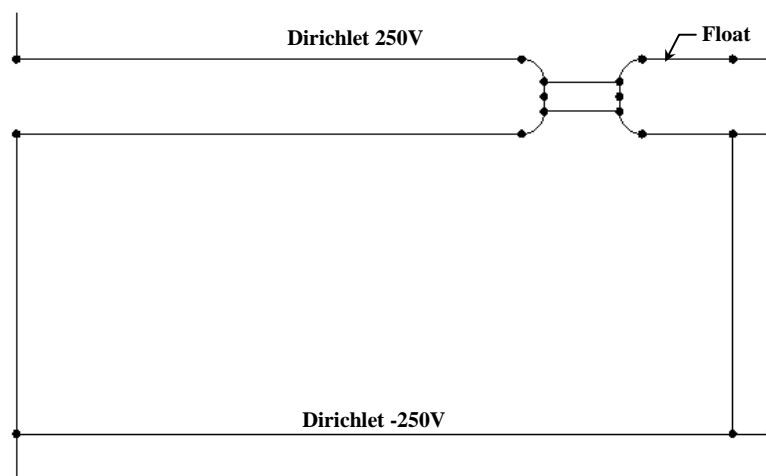
### Introduction

Three line regions are created to define the boundary conditions (LOWELEC, UPELEC, and RING).

### Boundary conditions

The boundary conditions of the problem are the following:

- **Dirichlet** conditions on the electrodes, in order to set the values of the electric potential:
  - $V = -250$  V on the lower electrode (LOWELEC line region)
  - $V = 250$  V on the upper electrode (UPELEC line region)
- **Float** condition on the outline of the guard ring (RING line region)



### Data

The characteristics of the line regions are presented in the table below.

Line region					
Name	Comment	Type		Expression	Color
LOWELEC	Line region modeling the lower electrode	Boundary condition: imposed electric potential	Formula with I/O parameters	-250	Magenta
UPELEC	Line region delimiting the upper electrode	Boundary condition: imposed electric potential	Formula with I/O parameters	250	Red
RING	Line region delimiting the guard ring	Perfect conductor with floating potential	-	-	Yellow



Physics → Line region → New



## 2.3.5. Assign line regions to lines

**Introduction** The line regions (LOWELEC, UPELEC and RING) are assigned to lines.

**Action** Assign line regions to lines.



Physics → Line region → Assign regions to lines

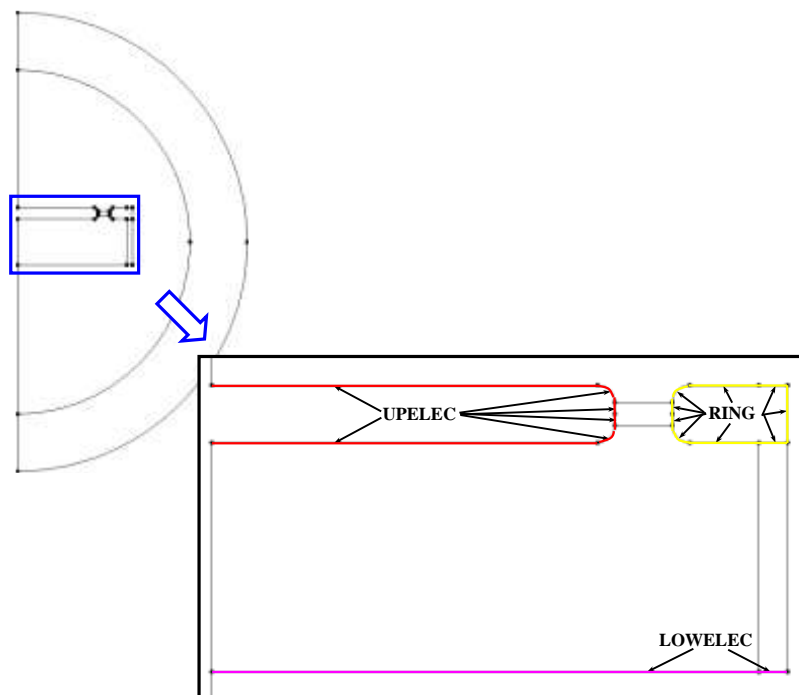


### Outline

The line regions are assigned as follows:

- the line region LOWELEC is assigned to the two lines represented the lower electrode
- the line region UPELEC is assigned to the six lines of the upper electrode
- the line region RING is assigned to the nine lines of the guard ring

The region assignment is presented in the figure below.



### 3. Case 1: static study

---

**Case 1**

*The first case is a static study.*

This study is a very easy problem of electrostatics of axisymmetric type. The testing liquid is pure water.

---

**Starting Flux project**

The Flux project is **GEO\_MESH\_PHYS.FLU**.

---

**New project**

The new Flux project is saved under the name CASE1.FLU

---

**Contents**

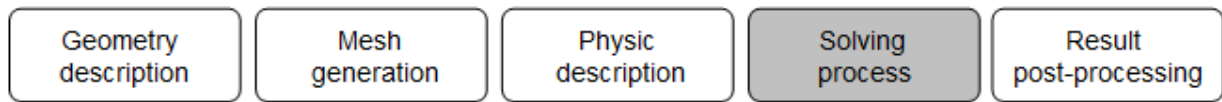
This chapter contains the following topics:

Topic	See Page
Case 1: solving process	37
Case 1: results post-processing	39

---



### 3.1. Case 1: solving process



---

**Goal**      The case 1 is solved using the default scenario with reference values.

---

**Action**      Solve CASE1.



Solving → Solve





## 3.2. Case 1: results post-processing

Geometry  
description

Mesh  
generation

Physic  
description

Solving  
process

Result  
post-processing

---

**Introduction** This section explains how to analyze the principal results of case 1.

---

**Contents** This section contains the following topics:

Topic	See Page
Display default graphic post processing	40
Display arrows of the electric field on a region boundaries	42
Compute the electric potential on a point	43
Compute the energy on LIQUID region	44
Plot a 2D curve of the electric field variation along a path	45
Plot a 2D curve of normal and tangential components of the electric field along a path	47
Plot a 2D curve of the electric field along a path	48

---

### 3.2.1. Display default graphic post processing

#### Goal

The display of graphic post processing enables the user to check if the problem is correctly formulated and emphasizes both the electric field concentration areas and the direction of the field. It also enables the user to check the mesh quality. This is the first, indispensable control of the accuracy of the results.

#### Action (1)

Display isovalues (4\_ISOVAL\_NO\_INFINITE)

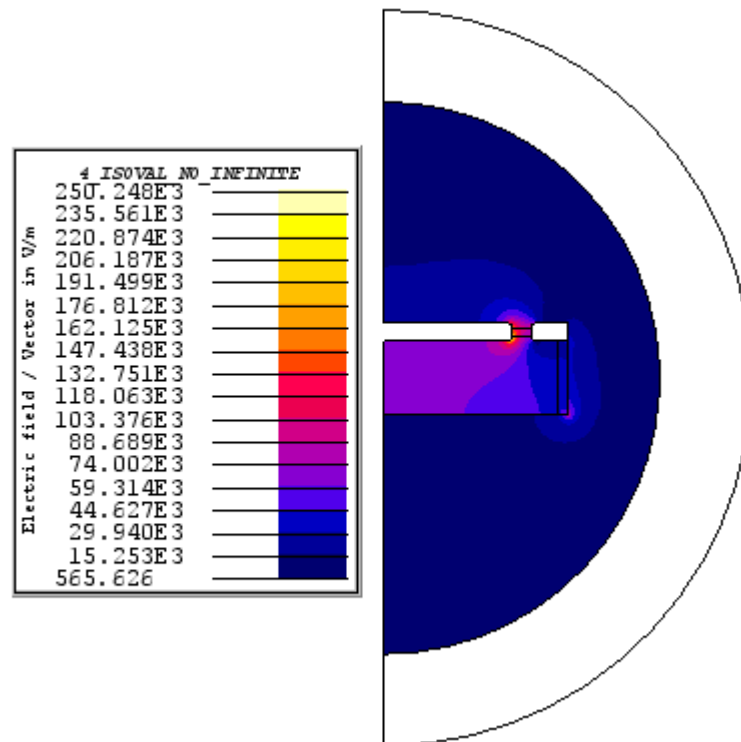


Graphic → Isovalues → Display isovalues



#### Result (1)

The isovalues of the electric field are displayed below.



#### Action (2)

Display isolines (4\_ISOLIN\_NO\_INFINITE)



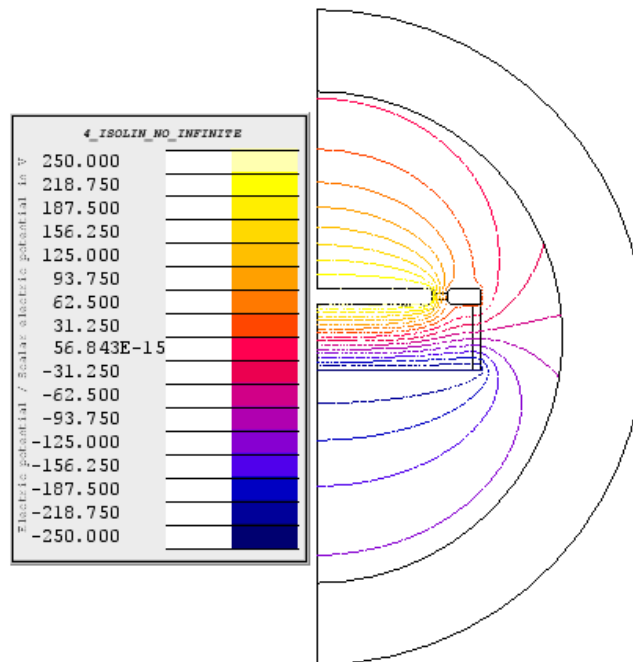
Graphic → Isolines → Display isolines



*Continued on next page*



**Result (2)** The isolines of the scalar electric potential are displayed below.



### 3.2.2. Display arrows of the electric field on a region boundaries

**Goal** The boundary vectors are used to visualize the value and the orientation of the electric field on the outline of a region.

**Data** The characteristics of the arrows are presented below.

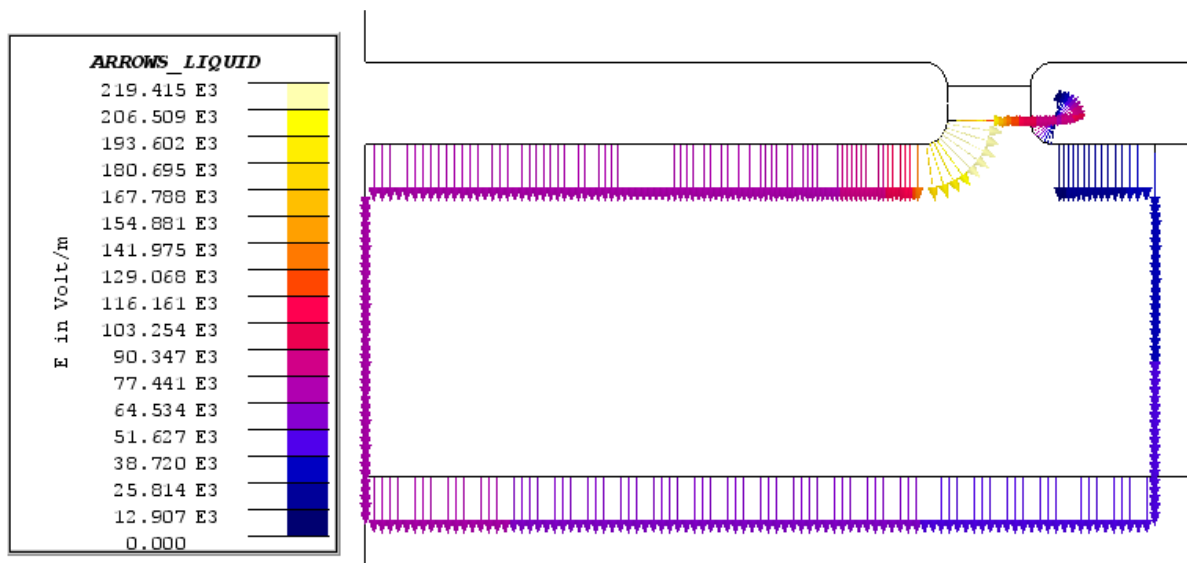
Arrows on boundary				
Name	Comment	Spatial group	Quantity	Formula
ARROWS_LIQUID	-	S_LIQUID	Electric field / Vector [V/m]	E



Graphic → Arrows boundary → New



**Result** The boundary vectors on the LIQUID region are displayed as presented in the figure below.



### 3.2.3. Compute the electric potential on a point

#### Goal

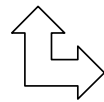
We will compute the local quantity:

- of the electric potential
- at the point with coordinates  $X = 13$  mm and  $Y = 0$  mm

#### Data

The characteristics of the computation are presented below.

Quantities computation on points			
Name	Comment	Quantity	Formula
POTENTIAL	Point in the LIQUID region	Electric potential / Scalar electric potential [V]	$V_e$



Point defined by its coordinates				
Coordinates		localization	Coord. system	Region
first	second			
13	0	no constraint	XY1	LIQUID

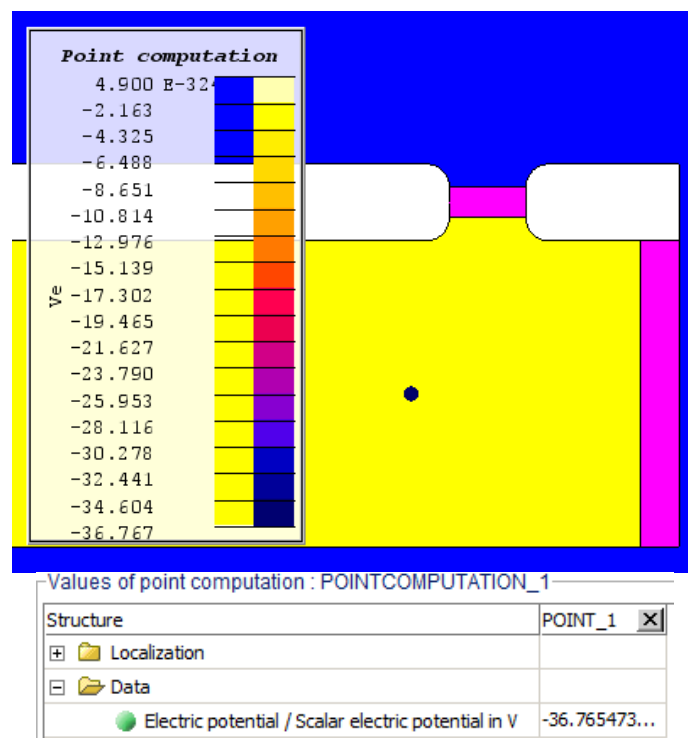


Computation → On point → New session Quantities computation on points



#### Results

The results are presented in the figures below.



### 3.2.4. Compute the energy on LIQUID region

**Goal** We will compute the local quantity:

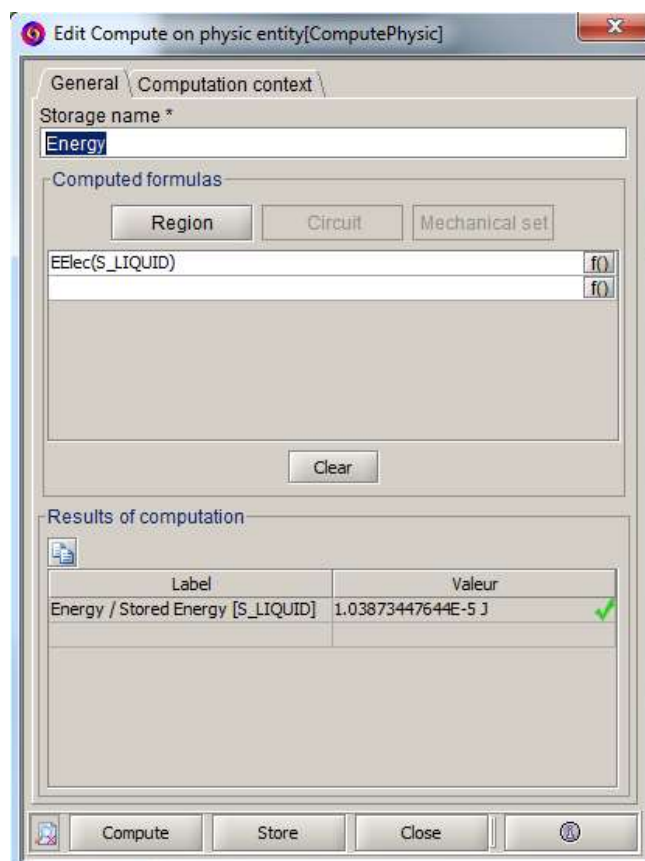
- of the energy
- on LIQUID region

**Data** The characteristics of the computation are presented below.

Computation on physical entity		
Name	Region	
	Group	Quantity
Energy	S_LIQUID	Energy / Stored Energy

☞ Computation → On physical entity → Compute

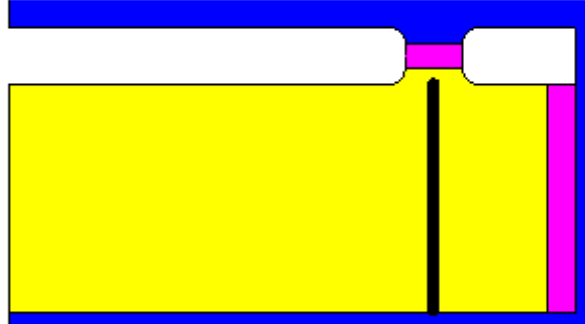
**Result** The result is presented in the figure below.



### 3.2.5. Plot a 2D curve of the electric field variation along a path

#### Goal

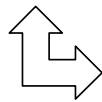
A 2D curve of the electric field along a path crossing the liquid region is computed and displayed.



#### Data (1)

The characteristics of the path are presented in the table below.

Path defined by 2 points			
Name	Comment	Definition	Discretization by intervals
LIQUID_PATH	Path in the LIQUID region	by coordinates	50



Path defined by coordinates					
Path points					
Starting point			Ending point		
Coord. system	Coordinates		Coord. system	Coordinates	
	First	Second		First	Second
XY1	15	4	XY1	15	-3.9



Support → Path → New → Add



#### Data (2)

The characteristics of the curve are presented in the table below.

2D curve (XYZ path)			
Name	Path	Quantity	Formula
ELEC_FIELD_LIQUID_PATH	LIQUID_PATH	Electric field / Magnitude [V/m]	ModV(E)



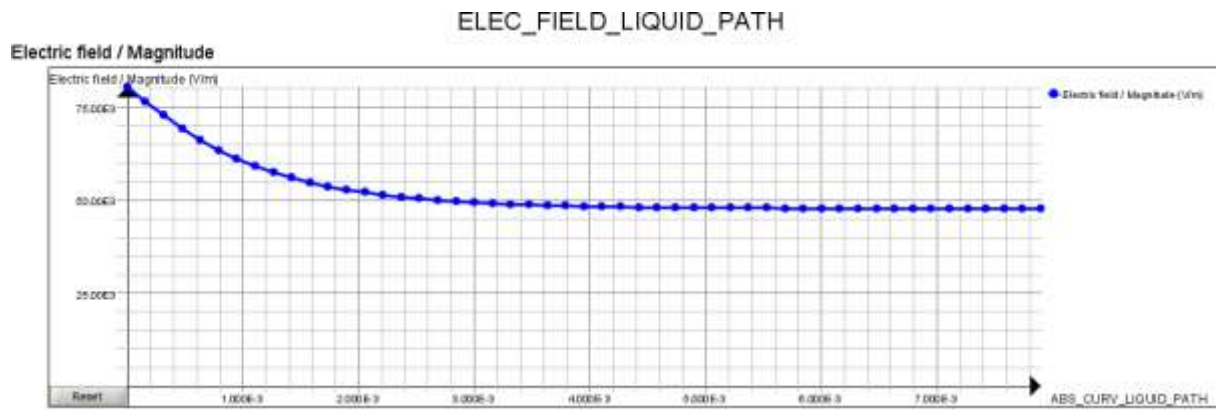
Curve → 2D curve (Path) → New 2D curve (Path)



*Continued on next page*

**Result**

The curve is displayed as presented in the figure below.



### 3.2.6. Plot a 2D curve of normal and tangential components of the electric field along a path

**Goal** We will plot the normal and tangential components of the electric field along the path already defined.

**Data** The characteristics of the curve are presented in the table below.

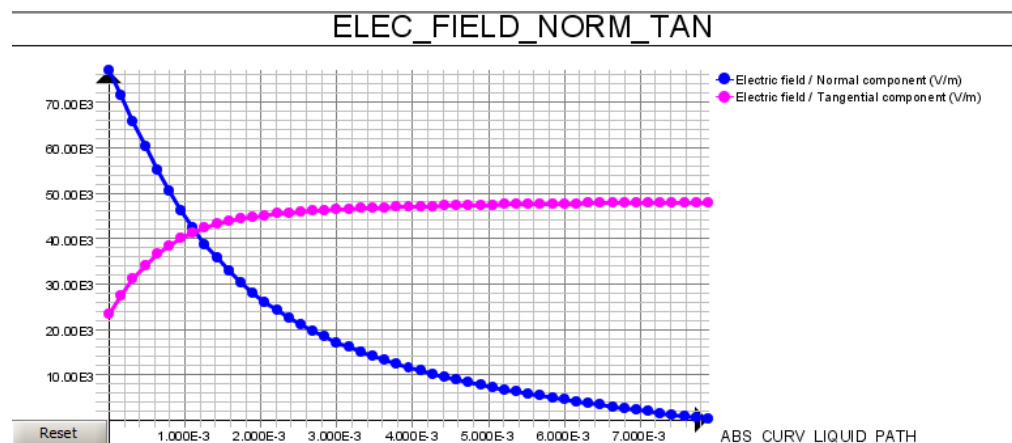
2D curve (XYZ path)		
Name	Path	Quantity
ELEC_FIELD_NORM_TAN	LIQUID_PATH	Electric field / Normal component
		Electric field / Tangential component



Curve → 2D curve (Path) → New 2D curve (Path)



**Result** The curves are displayed as presented in the figure below.

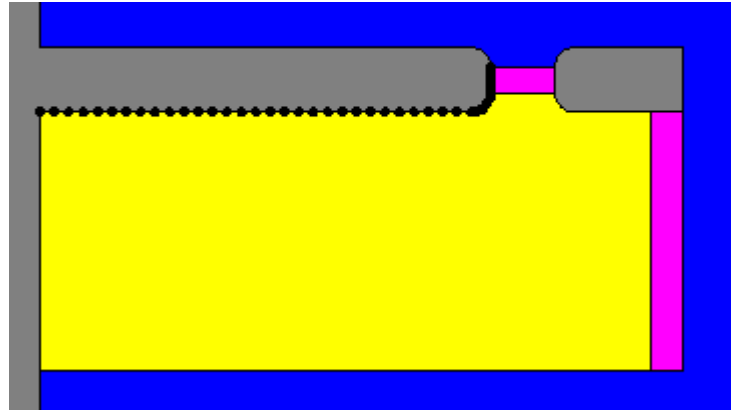


Note: display graph in absolute mode

### 3.2.7. Plot a 2D curve of the electric field along a path

#### Goal

A 2D curve of the relative permittivity along a path on the lines of the electrode is computed and displayed.



#### Data (1)

The characteristics of the path are presented in the table below.

Compound path			
Name	Type: Line	Region	Discretization by intervals
ELECT_PATH	Line 3	LIQUID	30
	Line 5	LIQUID	5
	Line 4	SPACER	5
	Line 16	SPACER	5



Support → Path → New



#### Data (2)

The characteristics of the curve are presented in the table below.

2D curve (XYZ path)			
Name	Path	Quantity	Formula
ELEC_FIELD_UPELEC_PATH	ELECT_PATH	Electric field / Magnitude	ModV(E)



Curve → 2D curve (Path) → New 2D curve (Path)

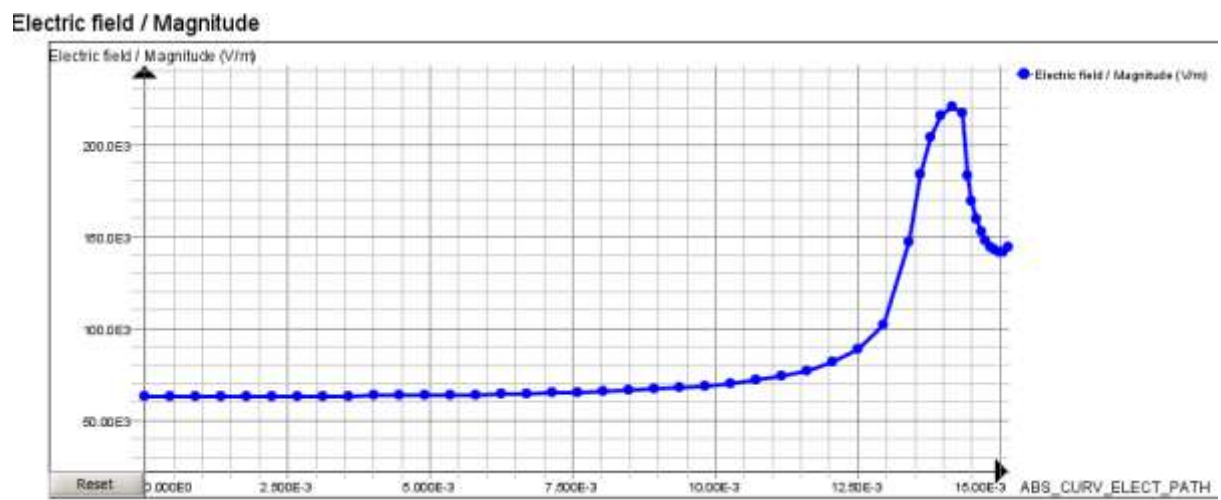


*Continued on next page*



**Result**

The curve is displayed as presented in the figure below.





## 4. Case 2: multi-parametric computation

### Case 2

*The second case is a multi-parametric computation.*

In this study two parameters – physical and geometric – are used. The physical parameter is the relative permittivity of the testing liquid (pure water) varying between 10 and 120. The geometric parameter is the curvature radius of the rounded corners of the electrodes varying between 0.6 mm and 0.8 mm. The last parameter determines the height of the upper glass spacer. The height of the upper spacer decreases when the value of the curvature radius increases.

### Starting Flux project

The Flux project is **GEO\_MESH\_PHYS.FLU**.

### New project

The new Flux project is saved under the name CASE2.FLU

### Contents

This chapter contains the following topics:

Topic	See Page
Case 2: physical description	53
Case 2: solving process	57
Case 2: results post-processing	59



## 4.1. Case 2: physical description

Geometry  
description

Mesh  
generation

Physic  
description

Solving  
process

Result  
post-processing

---

**Introduction** This section explains how to modify the initial physical description

---

**Contents** This section contains the following topics:

Topic	See Page
Create an I/O parameter	54
Modify a material	55
Create sensors	56

---

### 4.1.1. Create an I/O parameter

---

**Goal** A physical In/Out parameter is created. This parameter enables the variation of the relative permittivity of WATER material.

---

**Data** The characteristics of the I/O parameter defined by a scenario are described in the table below.

I/O parameters controlled via a scenario	
Name	Reference value
EPSR_WATER	80



Parameter/Quality → I/O Parameter → New



### 4.1.2. Modify a material

---

**Goal** The WATER material is modified in order to enter the changes produced by the I/O parameter creation.

---

**Data** The characteristics of the material modification are described in the table below.

D(E) dielectric property: linear isotropic		
Name	Comment	Relative permittivity
WATER	Pure water at 20 degrees	EPSR_WATER

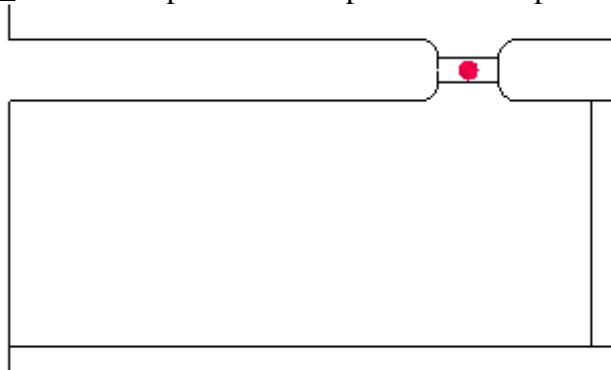
---

### 4.1.3. Create sensors

#### Goal

Three sensors are created on the same point. This point is located at the center of the spacer between the two electrodes

- MODE\_PT1 sensor permits to compute vector component of the electric field on the point
- VOLTAGE\_PT1 sensor permit to compute electrical potential on the point



#### Data

The characteristics of the sensors are described below.

Sensor: Point (a spatial quantity on a point)				
Name	Formula	Support: point		
		Coord. system	Coordinates	
			1st	2nd
MODE_POINT1	ModV(E)	XY1	15	5
VOLTAGE_POINT1	Ve		15	5



Parameter/Quality → Sensor → New





## 4.2. Case 2: solving process

Geometry  
description

Mesh  
generation

Physic  
description

Solving  
process

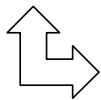
Result  
post-processing

**Introduction** This section explains how to prepare and solve case 2.

**Data** The characteristics of the solving scenario are presented in the table below.

Solving scenario		
Name	Comment	Type
SCENARIO1	study using geometrical and physical parameter	multi-values

Solving scenario					
Parameter control					
Controlled parameter	Type	Interval			
		Lower limit	Higher limit	Method	Step value
EPSR_WATER	Multi-values	10	120	Step value	10
RADIUS	Multi-values	0.6	0.7	Step number (lin)	5
	Multi-values	0.7	0.8	List of steps	0.7
					0.73
					0.77
					0.8



Solving → Solving scenario → New



Solving → Solve





## 4.3. Case 2: results post-processing

Geometry  
description

Mesh  
generation

Physic  
description

Solving  
process

Result  
post-processing

---

**Introduction** This section explains how to analyze the principal results of case 2.

---

**Contents** This section contains the following topics:

Topic	See Page
Display default graphic post processing at a selected parametric step	60
Create animation of isovalues of the electric field on face regions versus I/O parameter	61
Plot a 3D curve of the electric field at a point versus I/O parameters	62
Plot a 3D curve of the potential at a point versus I/O parameters	63
Plot a 3D curve of electric field along a path versus I/O parameter	64
Plot a 2D curve of the energy versus I/O parameter	66

---

### 4.3.1. Display default graphic post processing at a selected parametric step

**Goal** The default isovalues of the electric field are displayed in order to give information on its intensity and control the quality of the mesh.

**Data (1)** The characteristics\* of the computation step are presented in the table below.

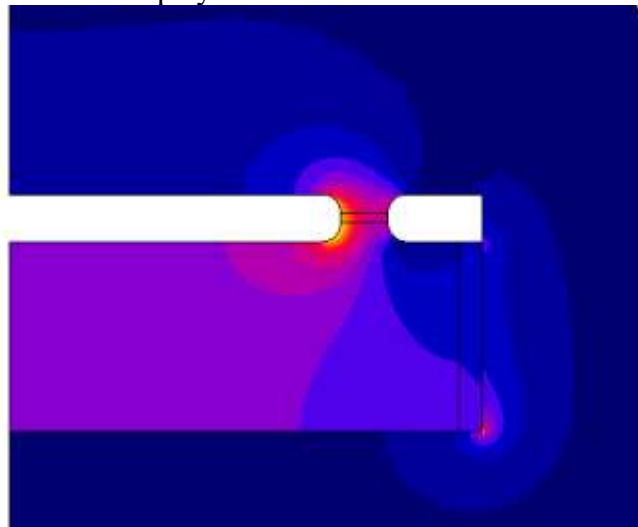
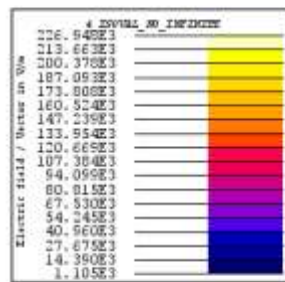
Scenario and computation step		
Scenario	Computation step	
	Parameter name	Value
SCENARIO_1	RADIUS	0.8
	EPSR_WATER	80

\* These characteristics are located in the dialog box below the data tree.

**Action** Display isovalues



**Result** The isovalues of the electric field are displayed below.



### 4.3.2. Create animation of isovalues of the electric field on face regions versus I/O parameter

**Goal** The animation of isovalues of the electric field for different values of the radius parameter is created.

**Data** The characteristics of the animation are presented in the table below.

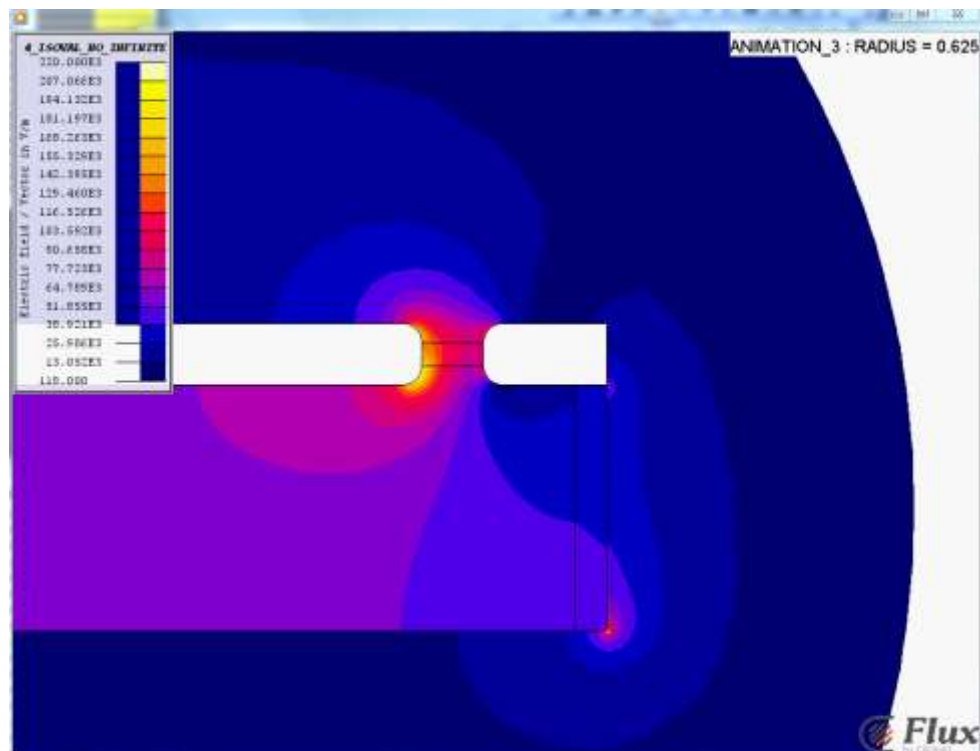
Animation							
Name	General (All Steps)					Display	
	Pilot: RADIUS				Build options	Isovalues	
	Parameters	Current value	min	max			
ANIMATION_1	EPSR_WATER	80			Build video	4_ISOVAL_NO_INFINITE	
	RADIUS		0.6	0.8		min	118
						max	220e3



Graphic → Animation → New



**Result** The animation video is created in the project repertory in a .AVI file.



### 4.3.3. Plot a 3D curve of the electric field at a point versus I/O parameters

**Goal** The values of the electric field as function of the relative permittivity and the curvature of the electrode's radius is computed and displayed in a 3D curve (I/O parameter).

**Data** The characteristics of the 3D curve are presented in the table below.

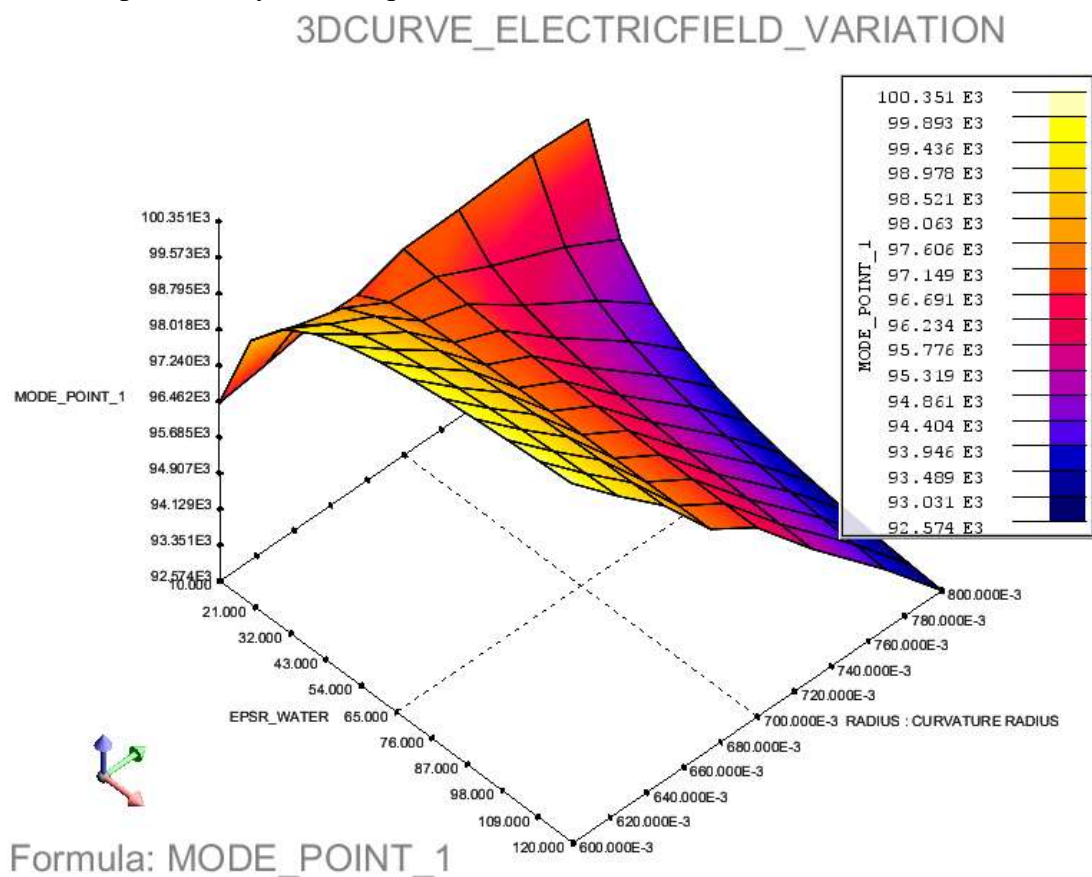
3D curve (2 I/O parameters)				
Name	Parameter			Formula f()
	Name	Limit min.	Limit max.	Sensor
3DCURVE_ELECTRIC FIELD_VARIATION	EPSR_WATER	10	120	MODE_POINT1
	RADIUS	0.6	0.8	



Curve → 3D Curve (2 I/O parameter) → New 3D Curve (2 I/O parameter)



**Result** The following diagram shows the electric field variation as function of the permittivity of the liquid and the radius of the electrode.



#### 4.3.4. Plot a 3D curve of the potential at a point versus I/O parameters

**Goal** The values of the electric potential as function of the relative permittivity and the radius of curvature of the electrode is computed and displayed in a 3D curve (I/O parameter).

**Data** The characteristics of the 3D curve are presented in the table below.

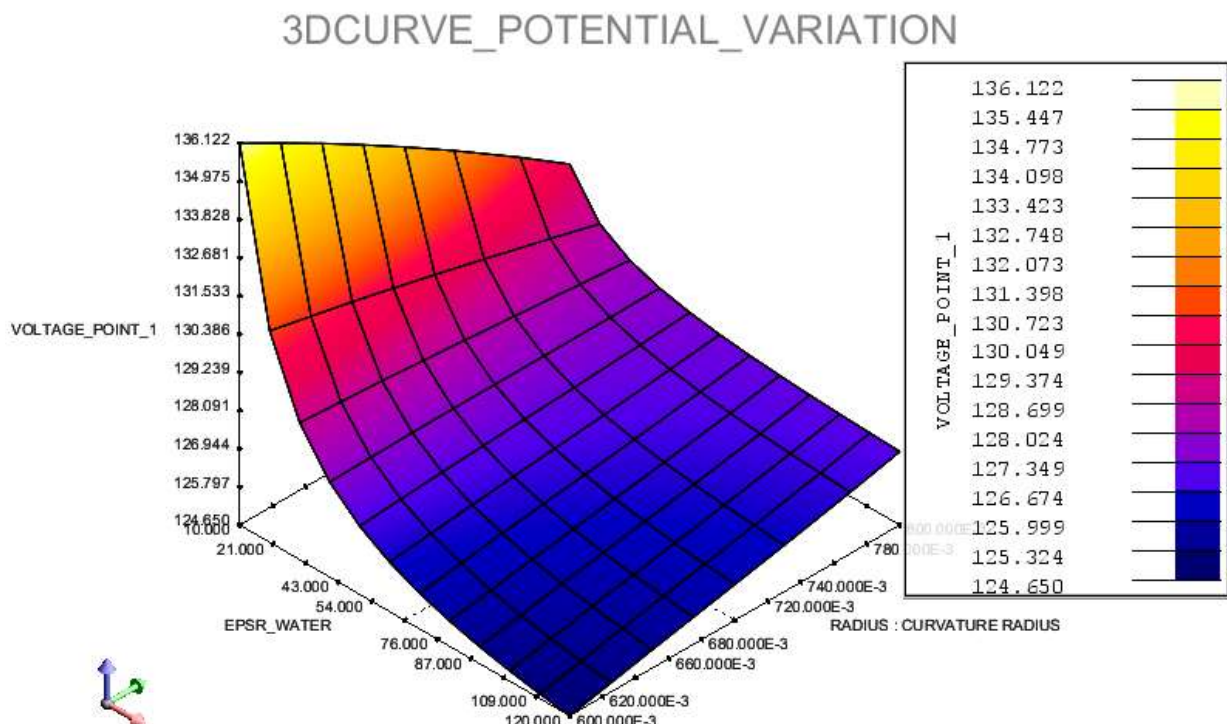
3D curve (2 I/O parameters)				
Name	Parameter			Formula
	Name	Limit min.	Limit max.	Sensor
3DCURVE_POTENTIAL_VARIATION	EPSR_WATER	10	120	VOLTAGE_PT1
	RADIUS	0.6	0.8	



Curve → 3D Curve (2 I/O parameter) → New 3D Curve (2 I/O parameter)



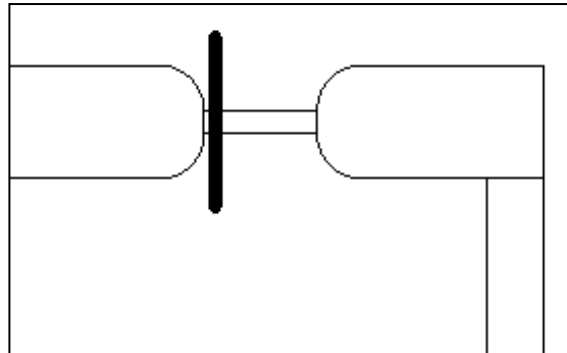
**Result** The following diagram shows the voltage variation as function of the permittivity of the liquid and the radius of the electrode.



### 4.3.5. Plot a 3D curve of electric field along a path versus I/O parameter

#### Goal

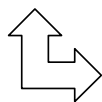
A path is created in order to plot a 3D curve of the electric field variation along a path as function of the curvature radius.



#### Data (1)

The characteristics of the path are presented in the table below.

Path defined by 2 points			
Name	Comment	Definition	Discretization
PATH_1	Crossing glass spacer	by coordinates	100



Path defined by coordinates					
Path points					
Starting point			Ending point		
Coord. system	Coordinates		Coord. system	Coordinates	
	First	Second		First	Second
XY1	14.2	3.5	XY1	14.2	6.5



Support → Path → New



#### Data (2)

The characteristics of the 3D curve are presented in the table below.

3D curve (Path + I/O parameter)						
Name	Path	Parameter				Quantity
		Name	Current value	Limit min.	Limit max.	
3D_CURVE_E_V_EPS	Path_1	EPSR_WATER	80			Electric field / Magnitude
		RADIUS		0.6	0.8	



Curve → 3D Curve (Path + I/O parameter) → New 3D Curve (Path + I/O parameter)

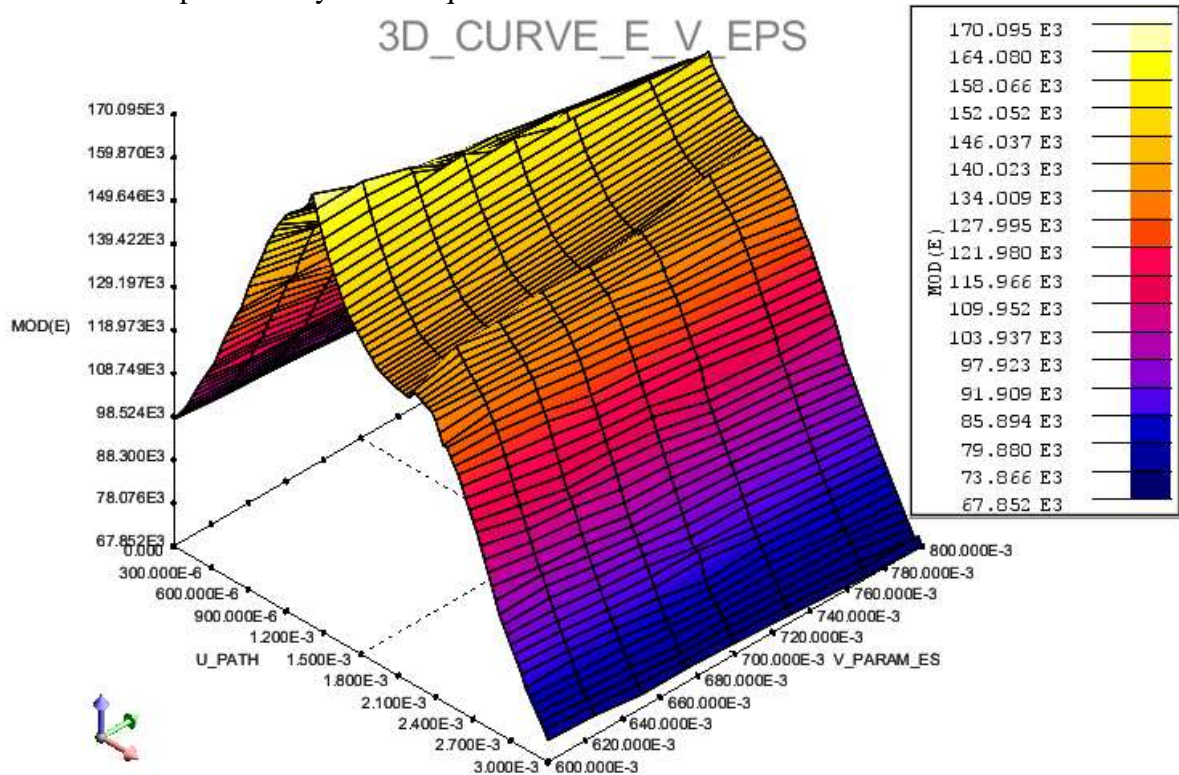


*Continued on next page*



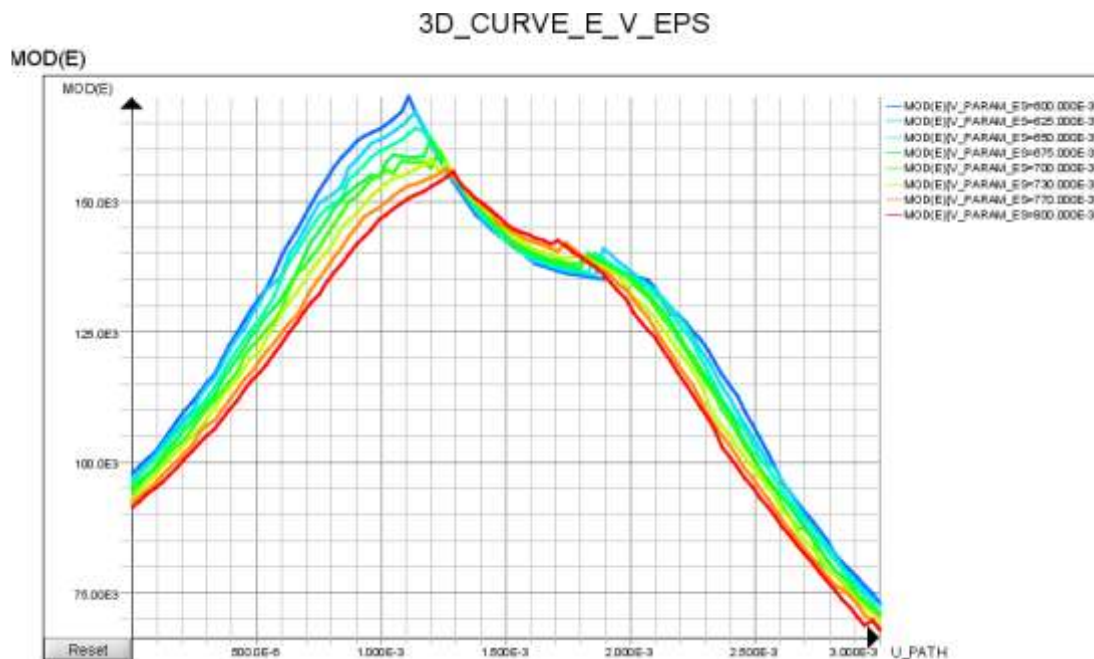
## Result

The following diagram shows the electric field variation as function of the permittivity of the liquid and the radius of the electrode.



Formula: MOD(E)

The results can also be displayed in a 2D representation



### 4.3.6. Plot a 2D curve of the energy versus I/O parameter

**Goal** The values of the energy stored in the SPACER region are computed as function of the permittivity.

**Data** The characteristics of the 2D curve are presented in the table below.

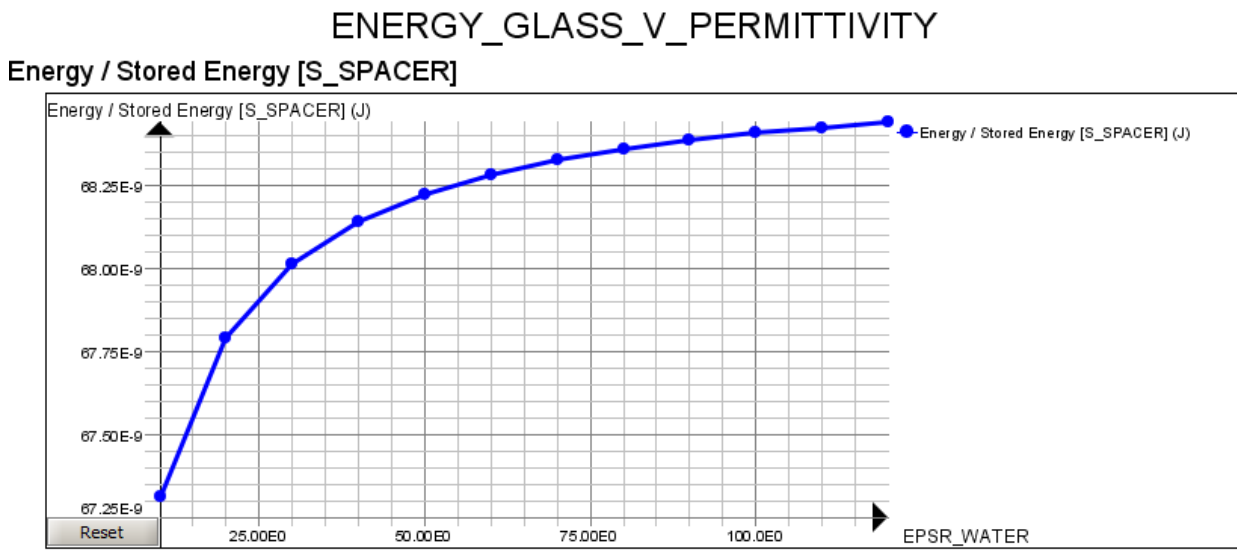
2D curve (I/O parameter)						
Name	Parameter				Region	
	Name	Current value	Limit min.	Limit max.	Spatial group	Quantity
ENERGY_GLASS_V_PERMITTIVITY	EPSR_WATER		10	120	S_SPACER	Energy / Energy stored
	RADIUS	0.8				



Curve → 2D Curve (I/O parameter) → New 2D Curve (I/O parameter)



**Result** The curve is displayed as presented in the figure below.  
Remark: choose a minimum stored energy displayed value of 67.25e-9J.



## 5. Case 3: static study, material with the low relative permittivity

---

### Case 3

*The third case is a static study.*

This study differs from case 1 only by the nature of the testing material.  
The testing liquid is mineral oil.

---

### Project name

The Flux project is **GEO\_MESH\_PHYS.FLU**.

---

### Starting Flux project

The new Flux project is saved under the name CASE3.FLU

---

### Contents

This chapter contains the following topics:

Topic	See Page
Case 3: modifying physical properties	69
Case 3: solving process	73
Case 3: results post-processing	75

---



## 5.1. Case 3: modifying physical properties

---

**Introduction** This section explains how to prepare case 3.

---

**Project name** The Flux project is **CASE3.FLU**.

---

**Contents** This section contains the following topics:

Topic	See Page
Create a material	70
Modify the LIQUID face region	71

---

### 5.1.1. Create a material

#### Goal

A new material is defined for the cell contents; the material is linear isotropic characterized by the relative permittivity.

#### Data

The characteristics of the materials are presented in the tables below.

D(E) dielectric property: linear isotropic		
Name	Comment	Relative permittivity
OIL	Mineral oil	2.5



Physics → Material → New



### 5.1.2. Modify the LIQUID face region

---

**Goal** The new OIL material is assigned to the LIQUID face region.

---

**Data** The characteristics of the materials are presented in the tables below.

Face region			
Name	Type	Matériau	Color
LIQUID	Dielectric region with charge source	OIL	Yellow

---





## 5.2. Case 3: solving process

---

<b>Introduction</b>	The case 3 is solved using the default scenario with reference values.
---------------------	--

---

<b>Action</b>	Solve case 3.
---------------	---------------



Solving → Solve
-----------------





## 5.3. Case 3: results post-processing

---

**Introduction** This section explains how to analyze the principal results of case 3.

---

**Contents** This section contains the following topics:

Topic	See Page
Display isolines of the electric potential on face regions	76
Plot a 2D curve of the electric field along a path	77
Import and superimpose 2D curve	79
Compute the energy on LIQUID region	81

---

### 5.3.1. Display isolines of the electric potential on face regions

**Goal** Isolines of the electric field are created in order to give information on its intensity and control the quality of the mesh.

**Data** The characteristics of the isolines are presented below.

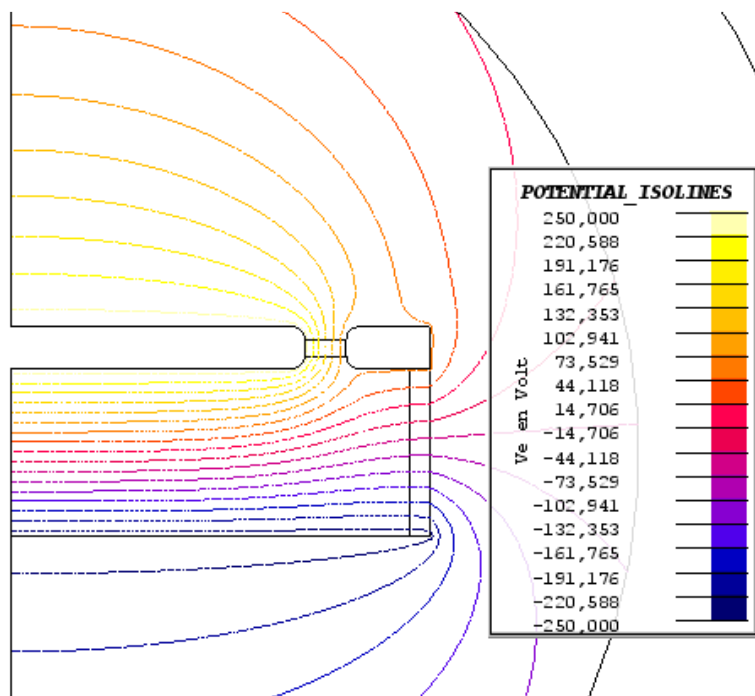
Isolines on face regions		
Spatial Group	Quantity	Formula
S_LIQUID	Electric potential / Scalar electric potential [V]	Ve
S_AIR		



Graphic → Isolines → New



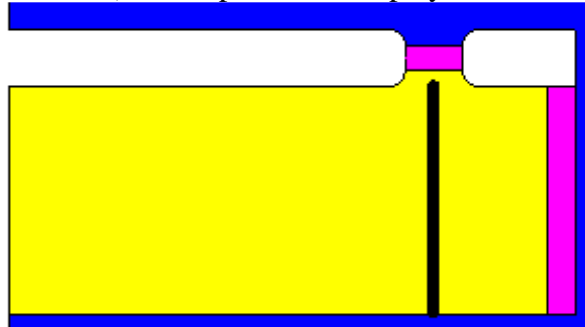
**Result** The isolines of the electric potential in the LIQUID and AIR regions are displayed below.



### 5.3.2. Plot a 2D curve of the electric field along a path

#### Goal

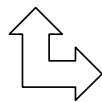
A 2D curve of the electric field along a path crossing the liquid region (already created in case 1) is computed and displayed.



#### Data (1)

The characteristics of the path are presented in the table below.

Path defined by 2 points			
Name	Comment	Definition	Discretization by intervals
LIQUID_PATH	Path in the LIQUID region	by coordinates	50



Path defined by coordinates					
Path points					
Starting point			Ending point		
Coord. system	Coordinates		Coord. system	Coordinates	
	First	Second		First	Second
XY1	15	4	XY1	15	-3.9



Support → Path → New



#### Data (2)

The characteristics of the curve are presented in the table below.

2D curve (XYZ path)			
Name	Path	Quantity	Formula
ELEC_FIELD_LIQUID_PATH	LIQUID_PATH	Electric field / Magnitude [V/m]	ModV(E)

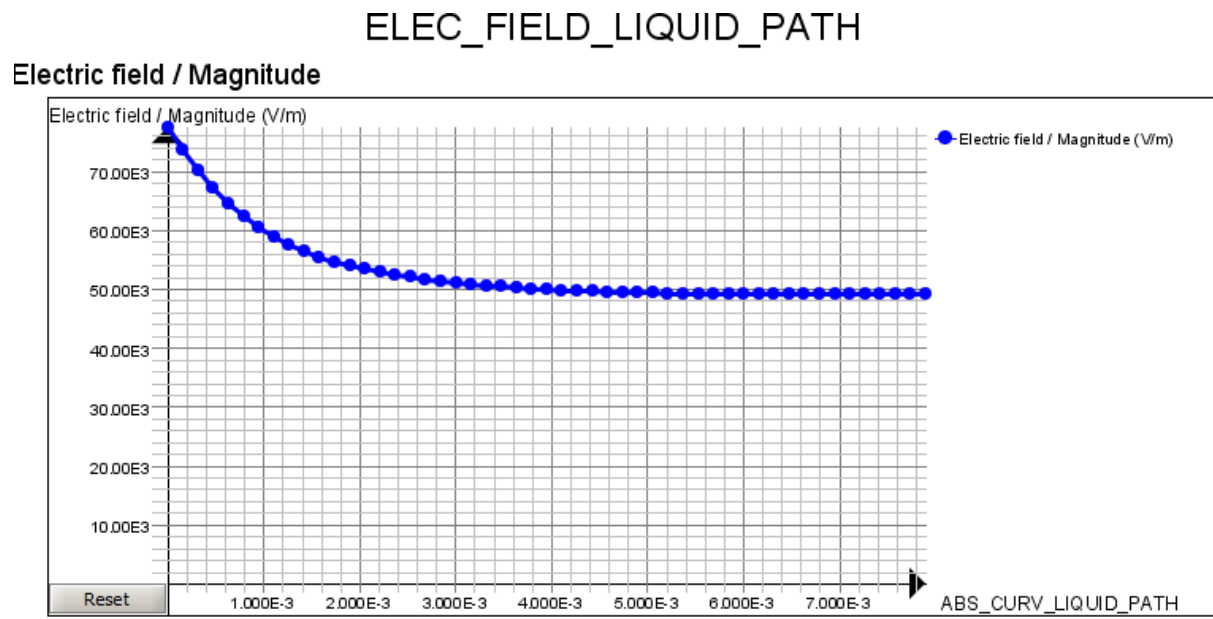


Curve → 2D curve (Path) → New 2D curve (Path)



**Result**

The curve is displayed as presented in the figure below.



### 5.3.3. Import and superimpose 2D curve

**Goal** The ELEC\_FIELD\_LIQUID\_PATH curve in case 1 is exported from the case 1 directory. Then this curve is imported in case 3 directory to compare it with the ELEC\_FIELD\_LIQUID\_PATH curve from case 3..

**Data (1)** The characteristics of the txt export from case 1 are presented in the table below.

TXT export (case 1)	
Name	Text file
ELEC_FIELD_LIQUID_PATH	ELEC_FIELD_LIQUID_PATH_case1.txt



Curve → 2D curve (Path) → TXT export

**Action** Import case 1 curve in case 3



Curve → 2D curve (Path) → Import a 2D curve – Flux file (txt)

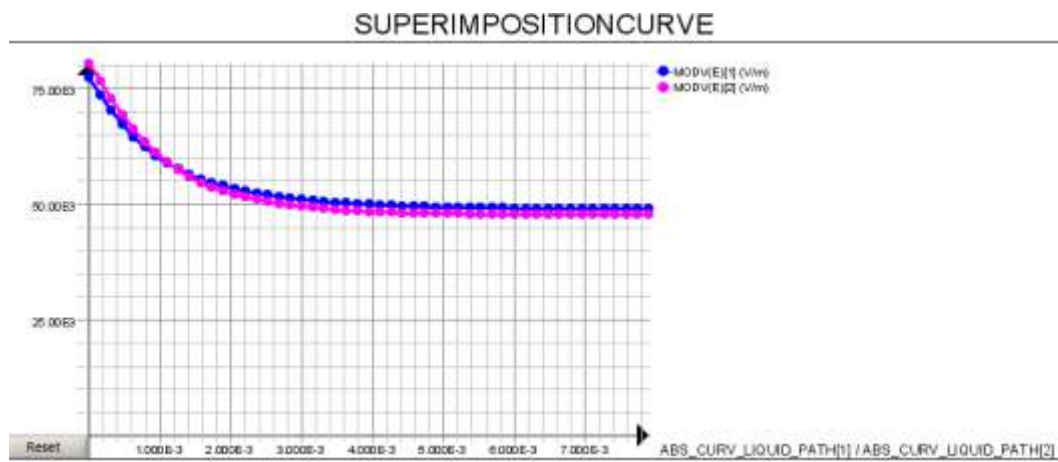
**Data (2)** The characteristics of the curves superimposition in case 3 are presented in the table below.

Superimpose 2D curves (case 3)		
Name	Interpolation	Curves
SuperimpositionCurve	Linear	ELEC_FIELD_LIQUID_PATH
		ELEC_FIELD_LIQUID_PATH_IMPORT_1



Curve → 2D curve (Path) → Superimpose 2D curves (path)

**Result** The superimposed curves are displayed as presented in the figure below.  
Remark: Choose the “Absolute” display mode



Display the graph in absolute mode



### 5.3.4. Compute the energy on LIQUID region

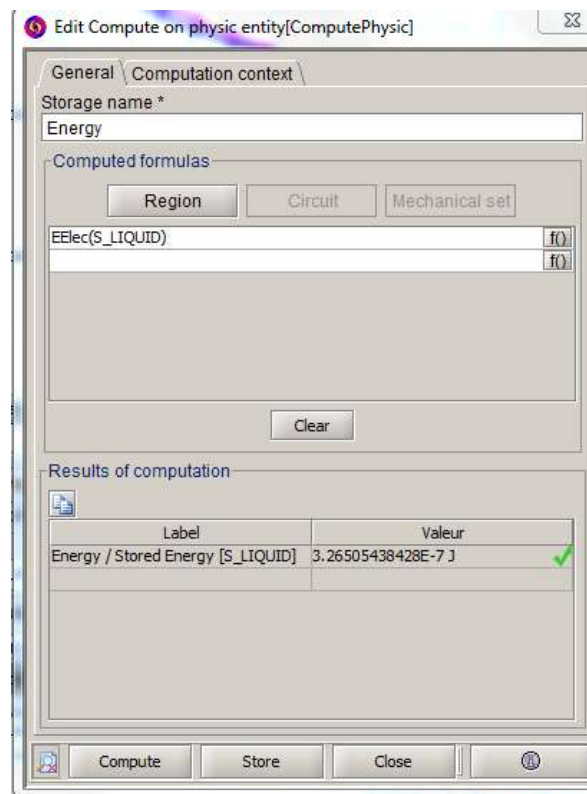
**Goal** We will compute the local quantity of the energy in the LIQUID region.

**Data** The characteristics of the computation are presented below.

Computation on physical entity		
Name	Region	
	Group	Quantity
Energy	S_LIQUID	Energy / Stored Energy

☞ Computation → On physical entity → Compute

**Result** The result is presented in the figure below.



Note: The energy stored in the LIQUID region is lower than the value corresponding to case 1 (roughly  $1.04e^{-5}$  J). Actually, compared to water the relative permittivity of the oil is lower.

